

High-fidelity simulations of transonic buffet on wide-span airfoils in the OpenSBLI automatic code-generation framework on GPUs

David J. Lusher*, Andrea Sansica, Markus Zauner, Atsushi Hashimoto (JAXA)

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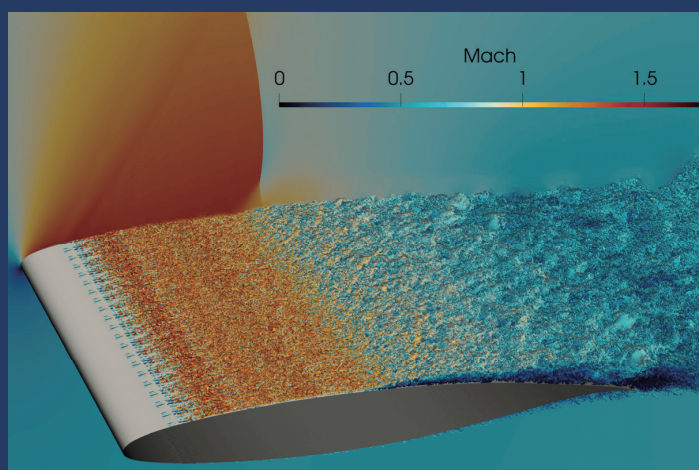
ANSS 55 Grand Numerical Prize Award Lecture - JAXA Chofu Aerospace Centre - November 21st 2023
第55回流体力学講演会／第41回航空宇宙数値シミュレーション技術シンポジウム 最優秀賞
*JSPS Postdoctoral Research Fellow & JSPS KAKENHI Grant: 22F2205



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- 中村さん, 上野さん, 松山さん, and all ANSS organising committee.
- JSS3 management and support team staff.



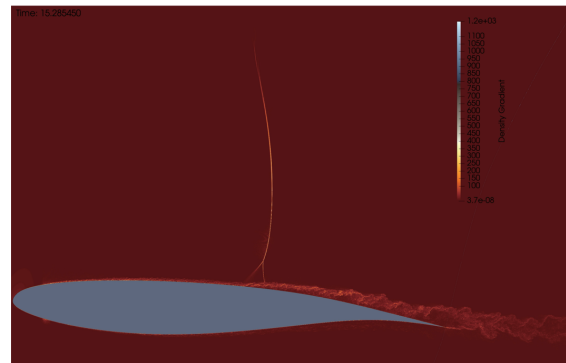
Wide-span turbulent transonic buffet simulation in OpenSBLI on the JAXA JSS3 GPU nodes

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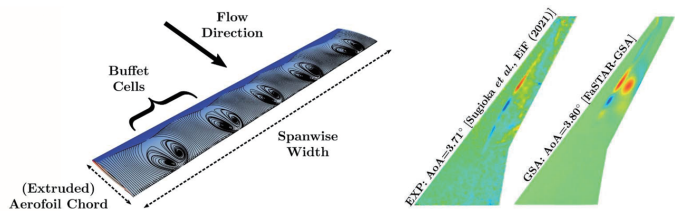


High-fidelity transonic buffet instabilities

- Transonic buffet is an aerodynamic instability that limits the flight envelope of aircraft.
- Depending on configuration, known to consist of:
 - a) A 2D **shock-oscillation** mode.
 - b) A 3D 'buffet cell' **span wise modulation** mode.
- Most computational studies are limited to **low-fidelity (RANS)-based methods**.
- High-fidelity (ILES/DNS) are very expensive, typically limited to narrow domains (Span ~ 5% chord length ~ 0.05 aspect ratio).
- Therefore, **only suitable for studying the 2D shock oscillations**.
- In this work, we apply ILES to **wider spans up to AR=3**, to search for 3D effects.



a) **2D shock oscillation instability**: OpenSBLI multi-block simulation of transonic buffet on infinite (span-periodic) OAT 15A wing segment, on 100 V100 GPUs on the JSS3 supercomputer.



b) **3D buffet cell instability**: [CFD: Sansica A., Hashimoto A. AIAA-J. 61(10) 2023]; [EXP: Koike et al. AIAA Aviation, 2016; Sugioka et al. Exp. In Fluids, 2018]

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Extruded wings comparison

Existing high-fidelity buffet studies: **Only 2D shock instability**

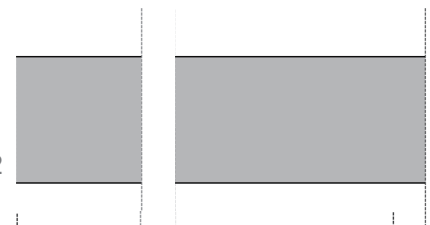
AR ~ 0.05 - 0.065



Current study:

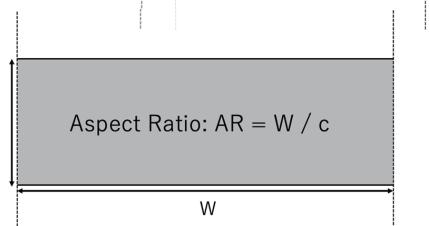
3D buffet cell instability

AR = 1, AR = 2



AR = 3

Aspect Ratio: $AR = W / c$

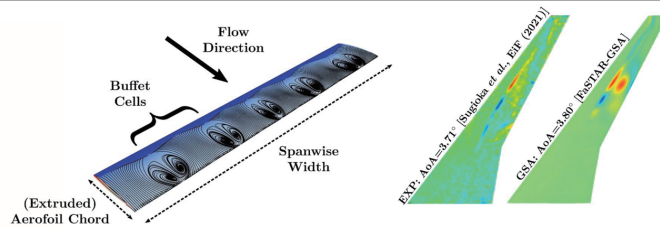


Open questions and previous studies

3D 'buffet cell' span wise modulation

• Previous studies:

- 3D instability is superimposed over the 2D shock-oscillation.
- **3D instability is dominant** for realistic configurations (finite-wings).
- Buffet cells convect with sweep angle.
- Q: Can we identify 3D effects in the absence of sweep (+ infinite wing)?
- **Lack of high-fidelity literature** for 3D buffet.
- Buffet cells / stall cells share similar features - Are they the **same phenomena** at different flow conditions?



3D buffet cell instability: [CFD: Sansica A., Hashimoto A. AIAA-J, 61(10) 2023];
EXP: Koike et al, AIAA Aviation, 2016; Sugioka et al. Exp. In Fluids, 2018]

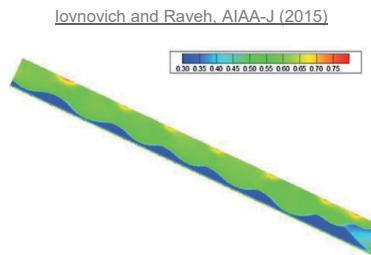


Fig. 26 Upper-surface-pressure coefficient snapshot: infinite-swept configuration, $b/c = 12$, and $\Lambda = 25$ deg nominal buffet conditions.

Plante et al., JFM (2021)

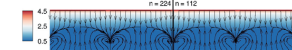


Figure 4.3 – Surface pressure coefficient and skin friction lines of 3-D steady solution with 224 (left) and 112 (right) spanwise grid cells (NACA4412, $M = 0.2$, $Re = 350\,000$, $\alpha = 15^\circ$, $\delta = 0^\circ$, $L_x = 6$).

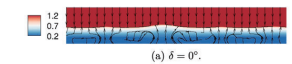


Figure 4.7 – Instantaneous surface pressure coefficient and skin friction lines for URANS simulations of infinite swept wings with two sweep angles (OALT25, $M = 0.7352$, $Re = 3 \times 10^6$, $\alpha = 4^\circ$, $L_x = 6$).

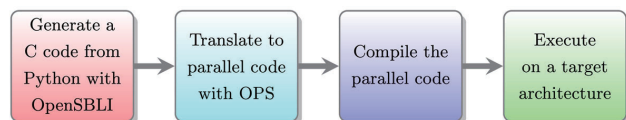
OpenSBLI Python-based code-generation

High-level problem specification via symbolic algebra

- OpenSBLI is a Python-based **code-generation** framework for compressible CFD using finite-differences [1].
- **Users specify the equations to solve** and simulation options in Python.
- **Symbolic algebra (SymPy)** is converted into a complete ILES/DNS CFD solver in **C/C++ code**.
- The OPS DSL enables parallel execution on many platforms (MPI/OpenMP/CUDA/...).
- Developed **2016-2021 (University of Southampton)**, during my PhD [1].
- New development at **JAXA, JSPS project (2022-2023) - next release & paper**.

```

1 ndim = 3
2 scl = """(scheme\A\Teno\)"
3 # Define the compressible Navier-Stokes equations in Einstein notation.
4 mass = "Eq(Der(rho,t), - Conservative(rho_j,x_j,ks))" % scl
5 momentum = "Eq(Der(rho_i,t), -Conservative(rho_i*u_j + KD(L_i,j)*p,x_j) + Der(tau_i,j,x_j))" % scl
6 energy = "Eq(Der(rho_e,t), - Conservative((p+rhoE)*u_j,x_j) + Der(q_i,x_i) + Der(u_i*tau_i,j,x_j))" % scl
7 stress_tensor = "Eq(tau_i,j, (mu/Re)*(Der(u_i,x_j) + Der(u_j,x_i) - (2/3)*KD(L_i,j)*Der(u_k,x_k)))"
8 heat_flux = "Eq(q_j, (-mu/(gamma-1)*MinF*MinFPrRe))*Der(T,x_j)"
9 # Numerical scheme selection
10 Avg = RoeAverage([0, 1])
11 LLF = LLFeno(teno_order, averaging=Avg)
12 cent = Central(4)
13 rk = RungeKuttaLS(3, formulation='SSP')
14 # Specify the boundary conditions
15 boundaries[direction][side] = IsothermalWallBC(direction, 0, wall_eqns)
16 # Generate a C code
17 alg = TraditionalAlgorithmRK(block)
18 OPSc(alg)
    
```



[1] D.J. Lusher, S.P. Jammy, N.D. Sandham. OpenSBLI: Automated code-generation for heterogeneous computing architectures applied to compressible fluid dynamics on structured grids. *Computer Physics Communications* (2021).

Oxford Parallel Structured (OPS) DSL

Automatic parallelisation for multi-block structured mesh applications

- OpenSBLI/OPS collaboration.
- The OPS library uses **source-to-source code translation** for structured mesh applications.
- OpenSBLI code written in the OPS API can be **automatically parallelised**.
- Supports C/C++/Fortran, to generate: MPI/OpenMP/CUDA/OpenCL/OpenACC/HIP
- **JSS3 TOKI-RURI & NASA Cluster** (Nvidia GPUs) -> CUDA+MPI+GPUDIRECT.
- **JSS3 TOKI-SORA & Fugaku** (A64FX CPUs) -> Hybrid MPI+OpenMP.

Parallel loop structure

```
int range4[] = {-3, b0np0 + 4, -3, b0np1 + 4, -3, b0np2 + 4};
ops_par_loop(ops_sbliblock00Kernel1064,
"Constituent Relations evaluation", ops_sbliblock00, 3, range4,
ops_arg_dat(ET_B0, 1, stencil_0_00, "double", OPS_READ),
ops_arg_dat(rho_B0, 1, stencil_0_00, "double", OPS_READ),
ops_arg_dat(u0_B0, 1, stencil_0_00, "double", OPS_READ),
ops_arg_dat(v0_B0, 1, stencil_0_00, "double", OPS_READ),
ops_arg_dat(w0_B0, 1, stencil_0_00, "double", OPS_READ),
ops_arg_dat(a_B0, 1, stencil_0_00, "double", OPS_WRITE),
ops_arg_dat(p_B0, 1, stencil_0_00, "double", OPS_RW));
```

Body of the function being called

```
void ops_sbliblock00Kernel1064(const ACC<double> &ET_B0, const ACC<double> &rho_B0,
const ACC<double> &u0_B0, const ACC<double> &v0_B0, const ACC<double> &w0_B0,
ACC<double> &a_B0, ACC<double> &p_B0)
{
double inv_rho = 0.0;
inv_rho = 1.0/rho_B0(0,0,0);
p_B0(0,0,0) = (gamma - 1) * (ET_B0(0,0,0) - 0.5*pow(u0_B0(0,0,0), 2)
- 0.5*pow(v0_B0(0,0,0), 2) - 0.5*pow(w0_B0(0,0,0), 2)) * rho_B0(0,0,0);
a_B0(0,0,0) = sqrt(gamma*inv_rho*p_B0(0,0,0));
```

Automatically generated CUDA GPU code

```
__global__ void ops_sbliblock00Kernel1064
{
__restrict__ arg0;
__restrict__ arg1;
__restrict__ arg2;
__restrict__ arg3;
__restrict__ arg4;
__restrict__ arg5;
__restrict__ arg6;
__restrict__ arg7;
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__restrict__ arg96;
__restrict__ arg97;
__restrict__ arg98;
__restrict__ arg99;
}
```

G. Mudalige, I. Reguly, M. Giles.

<https://op-dsl.github.io/>

I. Z. Reguly, G. R. Mudalige and M. B. Giles, Loop Tiling in Large-Scale Stencil Codes at Run-Time with OPS, in IEEE Transactions on Parallel and Distributed Systems, vol. 29, no. 4, pp. 873-886, 1 April 2018, doi: 10.1109/TPDS.2017.2778161.

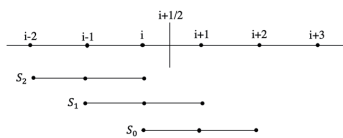
Summary of OpenSBLI numerical methods

Central + WENO shock-capturing

- **Non-dissipative (central) schemes** for high-resolution of turbulence and wave propagation.
- Convective terms written in cubic-split form to **improve numerical stability**.
- 5th order WENO-based shock-capturing is **applied only at shockwaves**.
- Dispersion-Relation-Preserving (DRP) filters are used in the freestream.
- Explicit 4th order low-storage Runge-Kutta time-stepping.

$$\frac{\partial \rho u \varphi}{\partial x} = \alpha \frac{\partial \rho u \varphi}{\partial x} + \beta \left(u \frac{\partial \rho \varphi}{\partial x} + \rho \frac{\partial u \varphi}{\partial x} + \varphi \frac{\partial \rho u}{\partial x} \right) + (1 - \alpha - 2\beta) \left(\rho u \frac{\partial \varphi}{\partial x} + \rho \varphi \frac{\partial u}{\partial x} + u \varphi \frac{\partial \rho}{\partial x} \right)$$

Cubic split-form of convective derivative operators for the compressible Navier-Stokes equations [1]



$$U^{n+1} = \hat{U}^{n+1} - \Delta t L_f(F)_{i,j,k}$$

$$L_f(F)_{i,j,k} = \frac{1}{\Delta x} \left[\tilde{F}_{j+1/2,k}^* - \tilde{F}_{j-1/2,k}^* \right] + \dots$$

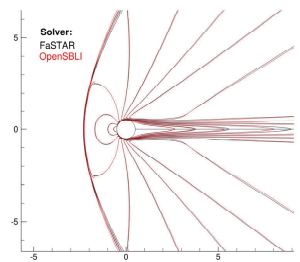
Staggered 5th order WENO shock-capturing stencil

Application of non-linear shock-capturing at the end of a full time-step [2]

Cross-validation of OpenSBLI to the FaSTAR code for supersonic cylinder flows.

Sansica, A, Lusher, D., Hashimoto, A. Mach Evolution of the Cylinder Wake Flow Bifurcations.

The 34th International Symposium on Shockwaves (ISSW34, South Korea 2023)



[1] G. Coppola et al. Journal of Computational Physics (2019).

[2] H. Yee et al. Computers & Fluids (2018).

OpenSBLI: Applications

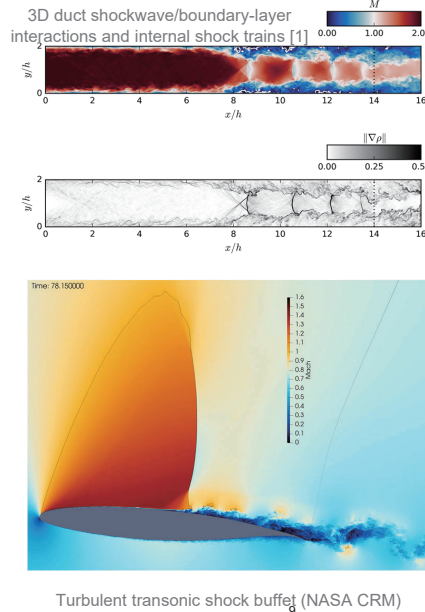
Compressible turbulence and shockwave/boundary-layer interactions

- Previous applications include **compressible turbulence**[2], 3D shockwave/boundary-layer interactions, shock-trains.
- Now extended to **multi-block for aerofoil and cylinder problems** (bottom, right).
- Successful **Fugaku FY2023 Junior Researcher project** completed.

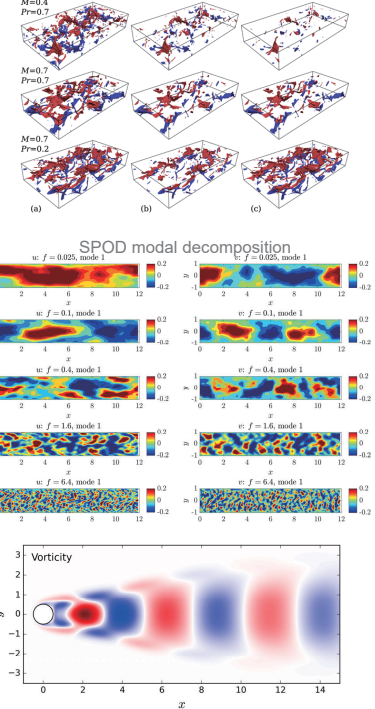
[1] A. Gillespie, N.D. Sandham. Shock Train Response to High-Frequency Backpressure Forcing. *AIAA Journal* 60 (6), 3736-3748

[2] D.J. Lusher, N.D. Sandham. Assessment of Low-Dissipative Shock-Capturing Schemes for the Compressible Taylor-Green Vortex. *AIAA Journal* (2021).

[3] A. Hamzehloo, D.J. Lusher, S. Laizet, N.D. Sandham. Direct numerical simulation of compressible turbulence in a counter-flow channel configuration. *Physical Review Fluids* 6 (9), 094603



Eddy shocklets in turbulent counter-flows [3].



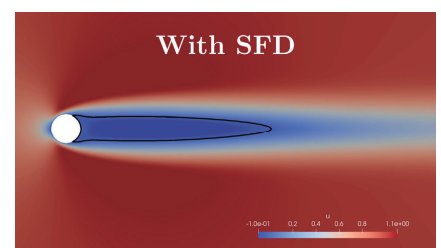
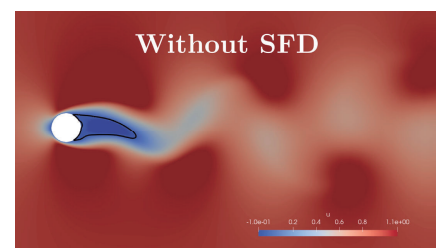
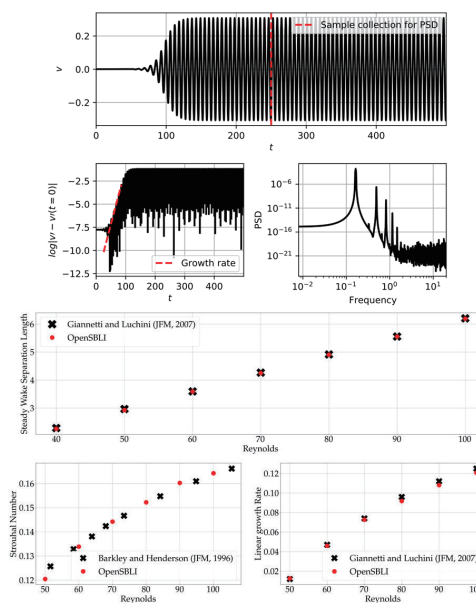
OpenSBLI: Recent validations

Cylinder and Airfoil validations in new OpenSBLI release

- Low Reynolds number ($Re=100$) validations against literature [1,2].
- Circular cylinder flows with Selective Frequency Damping (SFD).
- SFD demonstration with code and mesh in the release.

[1] F. Giannetti, et al. *Journal of Fluid Mechanics* 581 (2007).

[2] D. Barkley, et al. *Journal of Fluid Mechanics* (1996).



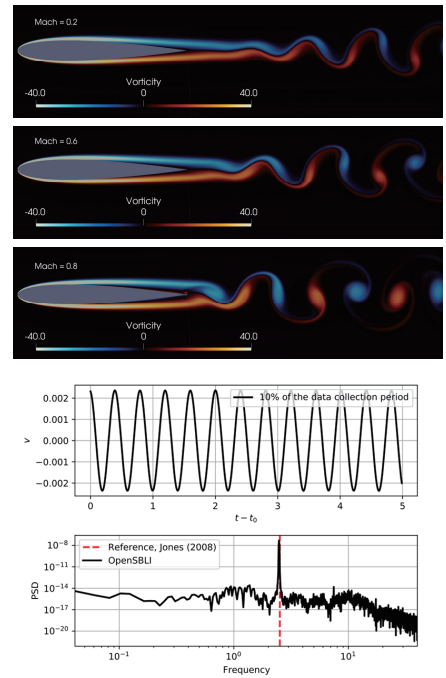
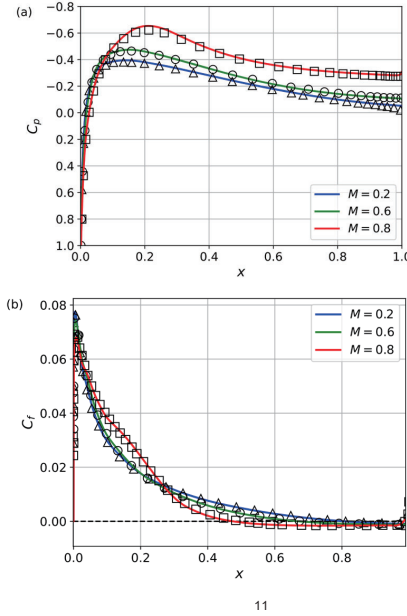
OpenSBLI: Recent validations

Cylinder and Airfoil validations in new OpenSBLI release

- Low Reynolds number ($Re=10,000$) validations against DNS data [1,2].
- NACA0012 airfoil.
- Open geometry can be contained in the code release.
- Airfoil demonstration with code and mesh

[1] L. E. Jones, Ph.D. thesis, University of Southampton (2008).

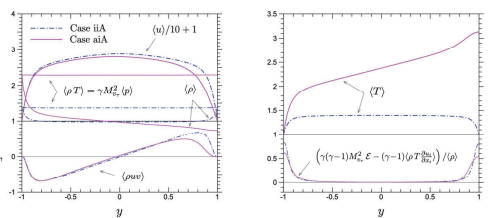
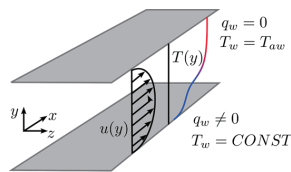
[2] L. E. Jones, Journal of Fluid Mechanics (2008).



OpenSBLI: Large-scale HPC on JAXA JSS3 GPUs

Using JSS3/Fugaku to generate high-quality DNS databases to improve RANS models at JAXA

- DNS of supersonic turbulence, **mixed isothermal/adiabatic** wall conditions within the same problem configuration [1].
- (JAXA): Dr. David J. Lusher, Dr. Andrea Sansica, Dr. Atsushi Hashimoto, Dr. Hiroyuki Abe.
- (NASA): Dr. Gary Coleman, (Boeing/Retired) Dr. Philippe Spalart.
- Generation of high-quality (**thermally balanced**) DNS databases of turbulent quantities.
- OpenSBLI DNS on JSS3 GPUs allows us to:
 - Validate lower-fidelity methods and boundary-conditions used in FaSTAR.
 - Improved understanding of terms such as the turbulent Prandtl number.
- Applied for **FY2024 Fugaku Junior Researcher Project**.



OpenSBLI mixed thermal wall conditions DNS: aIF2s (2201x787x1237)



[1] DJ Lusher, GN Coleman. Numerical Study of Compressible Wall-Bounded Turbulence—the Effect of Thermal Wall Conditions on the Turbulent Prandtl Number in the Low-Supersonic Regime. *International Journal of Computational Fluid Dynamics*, 1-19, (2023).

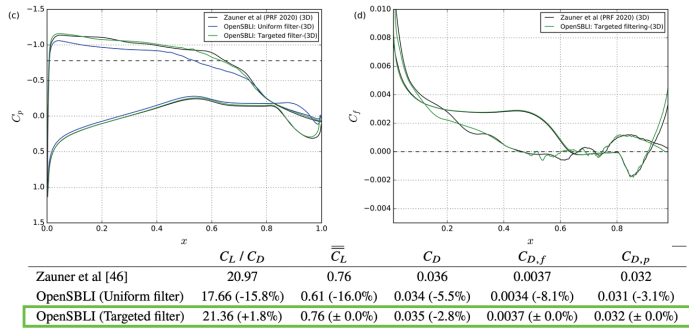
[2] D.J. Lusher, G.N. Coleman. Numerical Study of the Turbulent Prandtl Number in Supersonic Plane-Channel Flow – the Effect of Thermal Boundary Conditions. *NASA Technical Memorandum*, 10483 (2022).

Computational setup

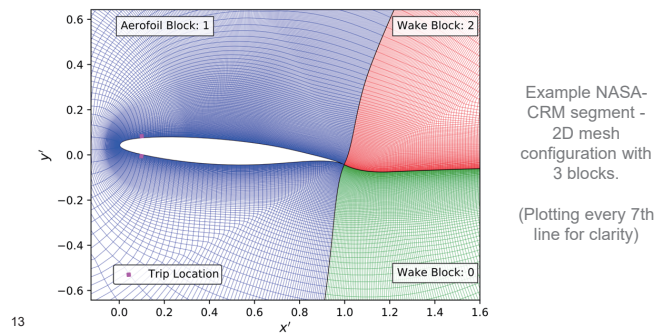
Multi-block mesh and flow parameters

- OpenSBLI was **validated for buffet** against literature for **Dassault Aviation V2C airfoil** [1].
- Using 3-block structured C-Mesh (Nx, Ny) plane points: (701,681), (2249,681), (701,681).
- Uniformly extruded in the span: 50-75 points per 0.05c width ~ **2.5 - 7.5 billion mesh points**.
- Narrow (0.05c) cases are extruded to generate **restart conditions for wide-span** (1c - 2c) cases.
- Flow conditions:
 - Moderate Reynolds number: 500,000.
 - Baseline Freestream Mach: 0.72.
 - AoA: 4 to 8 degrees.
 - **Zero sweep angle:** Q: Can we observe 3D effects without any imposed cross-flow?
 - **Turbulent buffet:** wall tripped at 0.1c chord.

$$\rho u_\eta|_{\eta=0} = \sum_{i=1}^3 A \exp\left(-\frac{(x-x_i)^2}{2\sigma^2}\right) \sin\left(\frac{k_i z}{0.05c}\right) \sin(\omega_i t + \Phi_i)$$



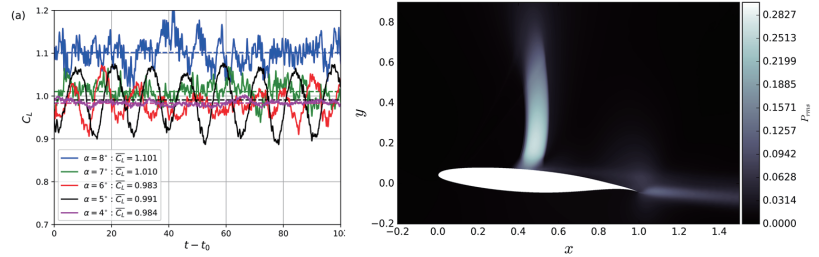
[1] Lusher D., et al. Automatic Code-Generation to Enable High-Fidelity Simulations of Multi-Block Airfoils on GPUs. AIAA SciTech 2023.



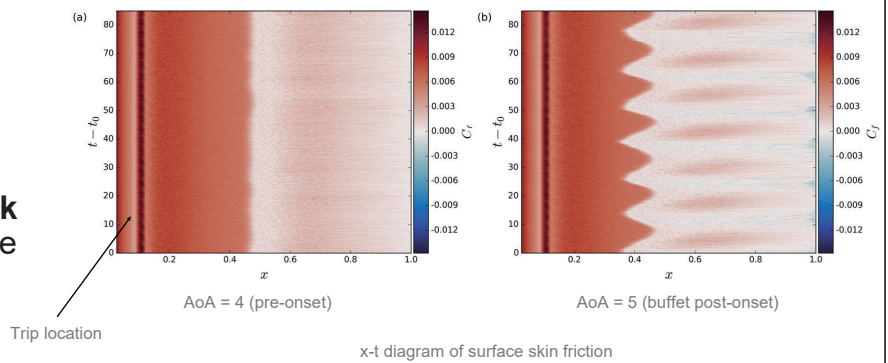
Narrow Domain: AoA Study

Time histories of surface skin-friction

- 2D (shock oscillation) buffet **onset conditions** are investigated with 3D simulations at AR=0.05.
- Range of: 4-8 degrees AoA.
- Time history (x-t) plot of surface **skin-friction**.
- AoA = 4 (pre-onset): **fixed shock location**.
- AoA = 5 (buffet onset): **shock oscillates** on the suction side



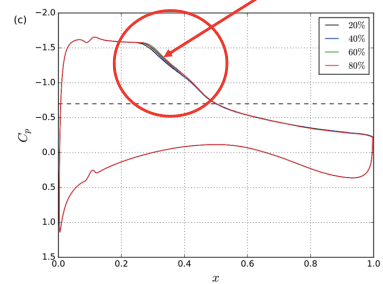
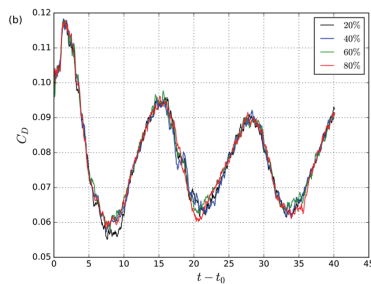
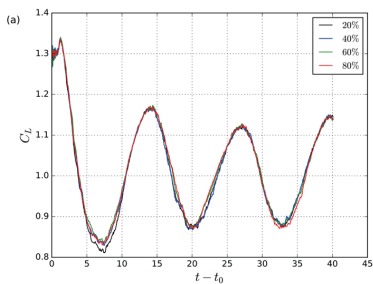
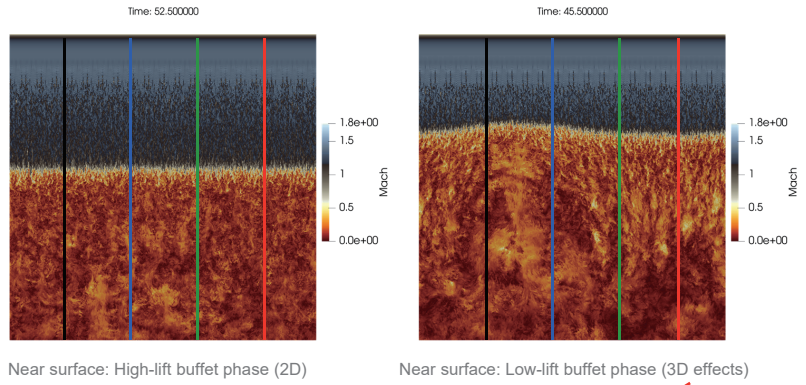
Time history of aerodynamic lift coefficient and RMS of pressure.



Extrusion to wide-span: AR1

Wide-span buffet effects no longer purely 2D

- AR=1 case, $M=0.72$, AoA : 6 degrees.
- 2.5 billion mesh points at AR=1
- At AR=1: the flow is no longer strictly 2D across the span.
- Large 3D separation bubbles occur, during low-lift phases.
- Sectional plots across the span (bottom) show the lack of span homogeneity.
- Seem to be linked to the point of maximum flow separation (low-lift).

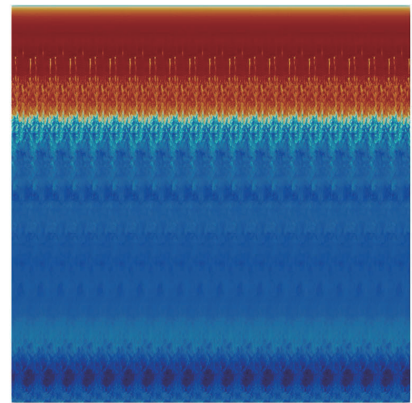


Extrusion to wide-span: AR1, AoA: 8

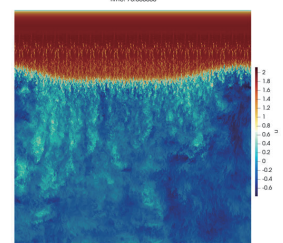
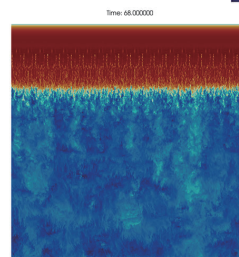
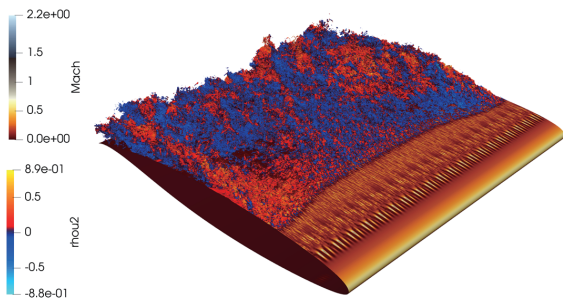
Wide-span buffet effects no longer purely 2D

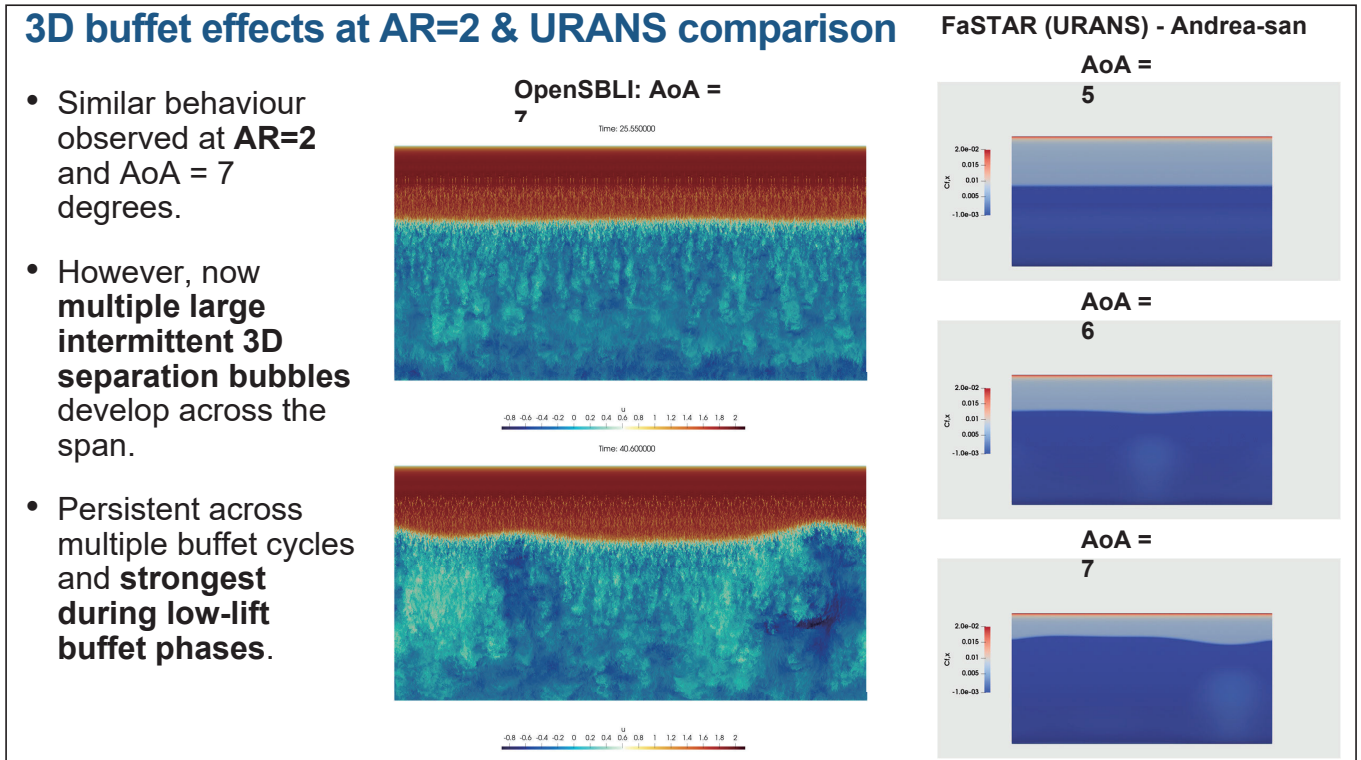
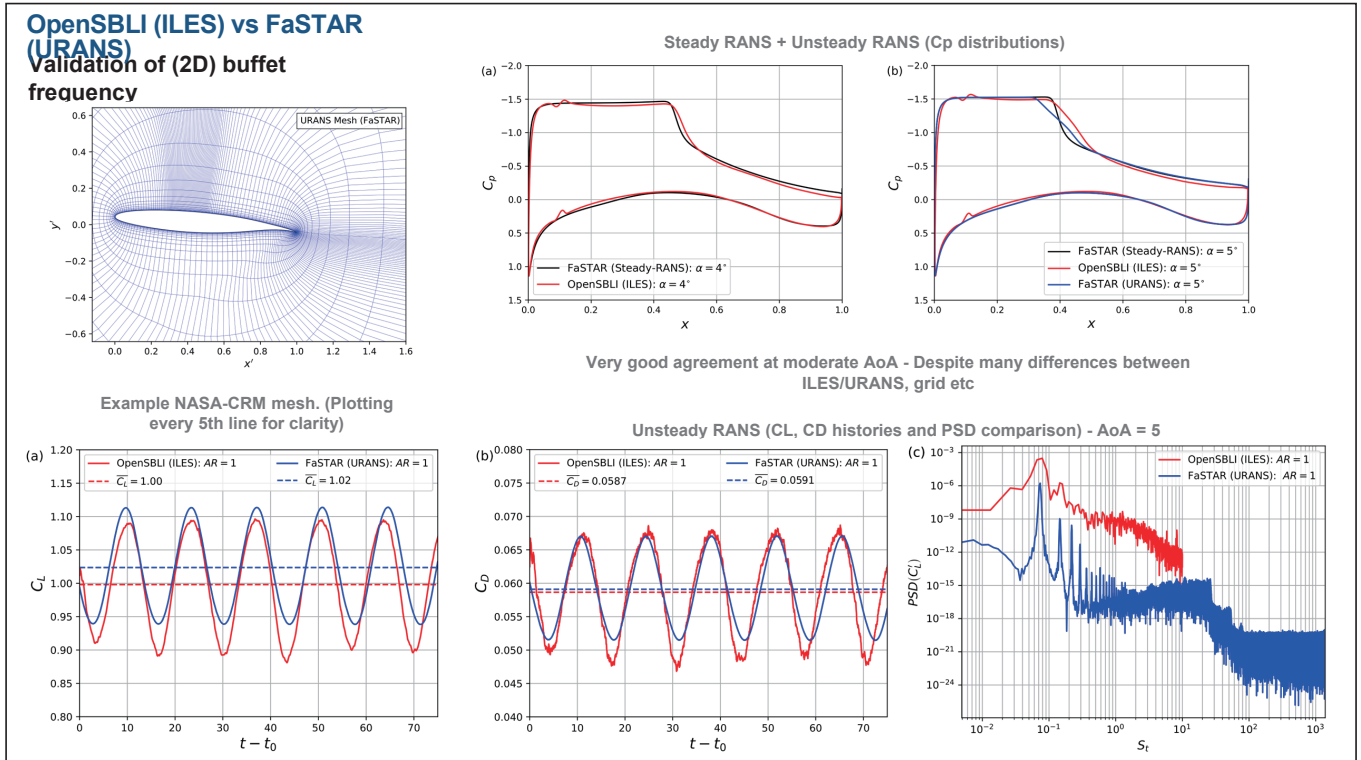
- AR=1 case, $M=0.72$, AoA : 8 degrees.
- At AR=1: the flow is no longer strictly 2D across the span.
- Large 3D separation bubbles occur, during low-lift phases.
- Seem to be linked to the point of maximum flow separation (low-lift).
- Curvature of the shock front (no longer 2D planar shock)

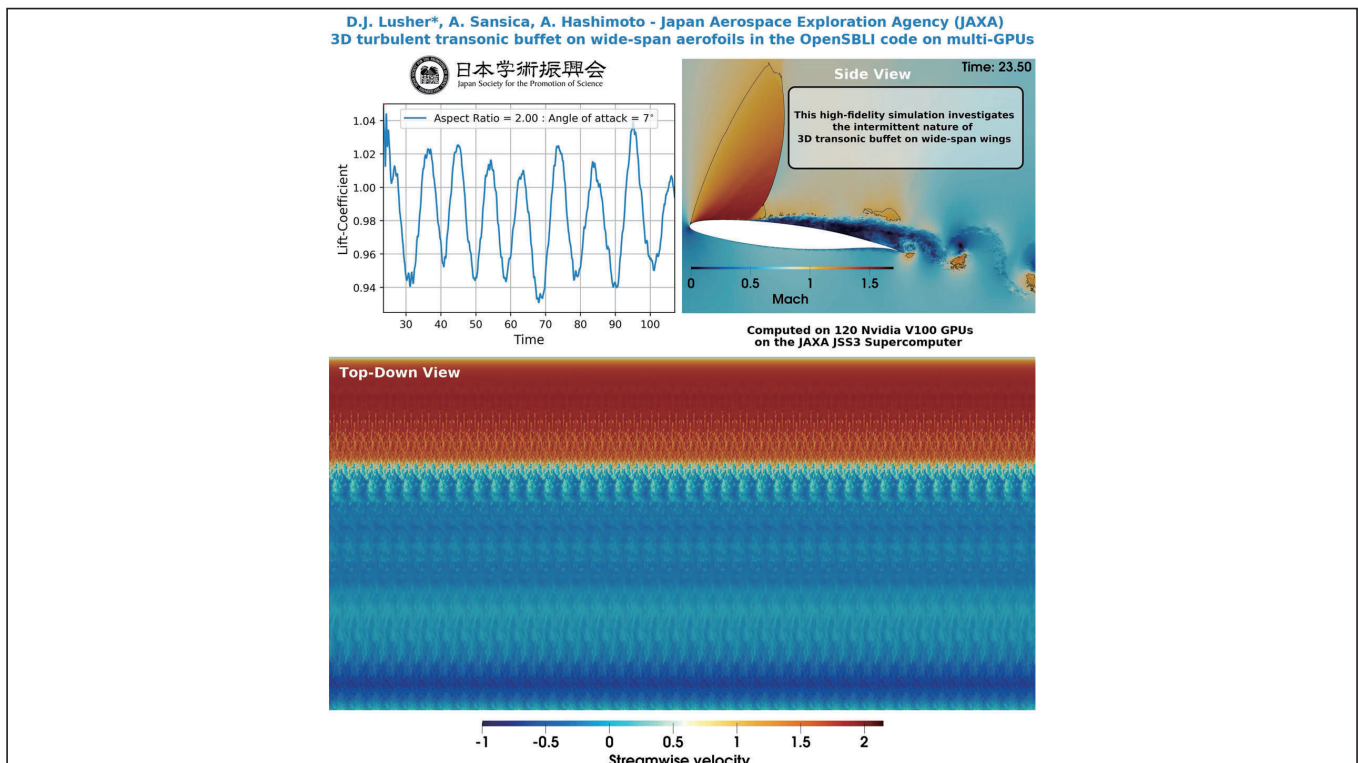
Time: 63.750000



Time: 75.500450







Conclusions & Summary

- Q: Can we observe 3D buffet effects for infinite (periodic) wings with zero sweep? - Yes, **at sufficiently wide aspect ratios**.
- World first high-fidelity **3D wide-span turbulent transonic buffet** simulations were performed on JSS3 GPU nodes, for NASA-CRM extruded wings at $Re = 500,000$ and Mach 0.72.
- **Large simulations on $N > 10^9$ mesh points**.
- Parametric study showed **2D shock oscillation buffet onset** occurs between 4-5 degrees AoA at **AR=0.05**.
- At **wide-span (AR=1,2,3)**, large **3D separation bubbles** form during low-lift phases, these **cannot be captured by narrow-span simulations**.
- They lead to **span-wise inhomogeneous curvature of the main shockwave**.
- We show that **narrow span simulations are not sufficient** to fully capture buffet phenomenon.
- Outlook: **Applying Modal Decomposition Methods (SPOD/DMD)**, publishing results.

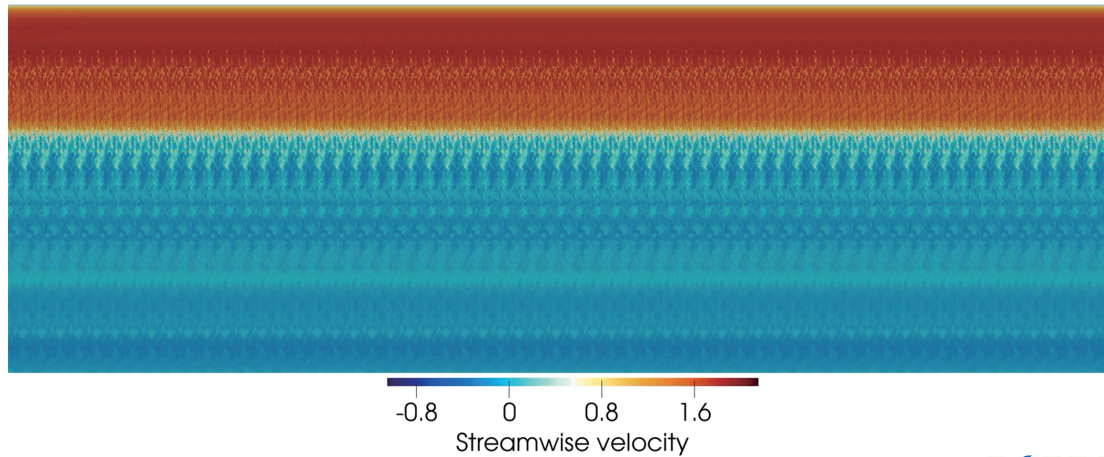
Contact: lusher.david@jaxa.jp. More information on the OpenSBLI code (<https://github.com/opensbli/opensbli>): D.J. Lusher, S.P. Jammy, N.D. Sandham. OpenSBLI: Automated code-generation for heterogeneous computing architectures applied to compressible fluid dynamics on structured grids. Computer Physics Communications (2021).

This work is funded by a JSPS postdoctoral fellowship and JSPS KAKENHI Grant: 22F2205. Computational time was provided by the JAXA JSS3 supercomputing facility and associated support staff, and the Fugaku supercomputer at RIKEN on projects hp220195, hp220226.

Thank you - Questions?

Aspect ratio AR=3, AoA = 6

Time: 159.50



Contact: lusher.david@jaxa.jp. More information on the OpenSBLI code (<https://github.com/opensbli/opensbli>): D.J. Lusher, S.P. Jammy, N.D. Sandham. **OpenSBLI: Automated code-generation for heterogeneous computing architectures applied to compressible fluid dynamics on structured grids.** Computer Physics Communications (2021).

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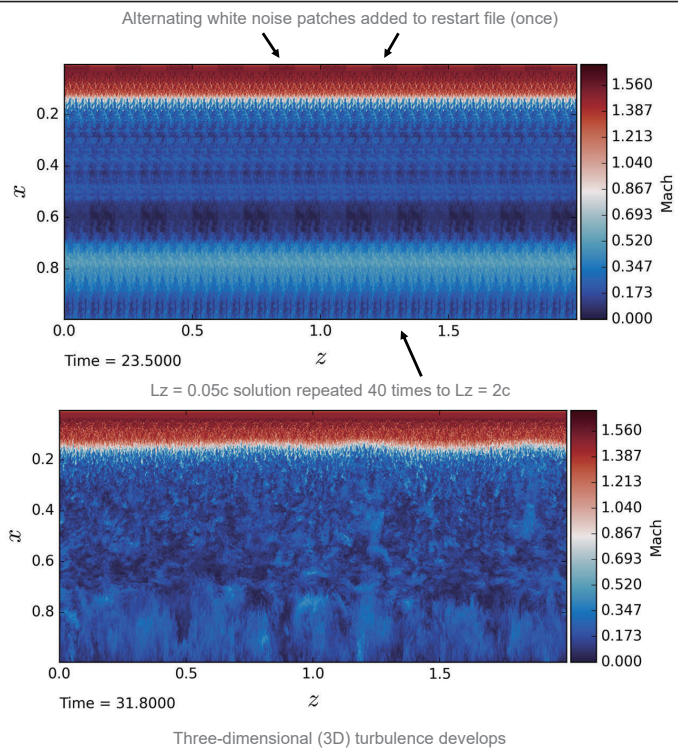
Extra

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Extrusion to wide-span: initial condition

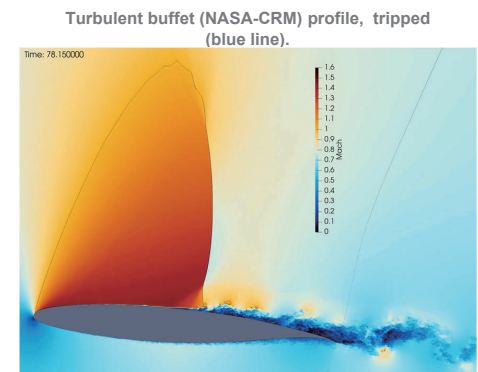
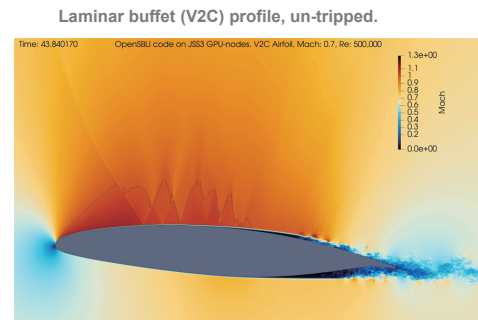
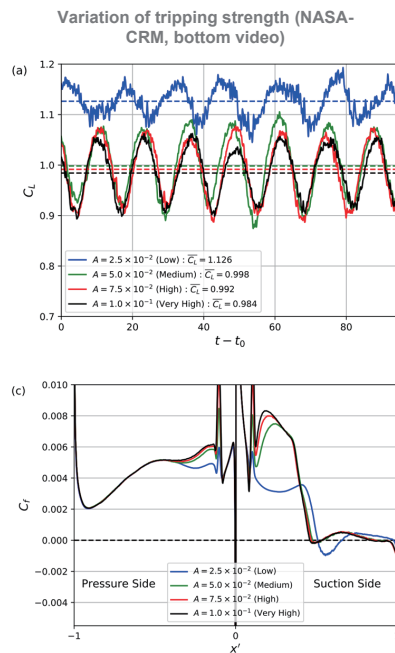
Avoiding long expensive transients

- Due to span wise periodic boundary condition, wide-span simulations can be **initialised with the fully developed narrow-domain flow-fields**.
- 0.05c profile is **repeated across the span 20-60 (AR1-AR3) times**.
- White noise is added to the boundary-layer once into the restart file to help **break symmetry quickly**.
- No long wavelengths are forced, large 3D effects develop naturally.



Influence of forcing amplitude - IUTAM 2024

- Plan to submit work to **IUTAM 2024 conference**.
- Varying the **strength of the tripping** on buffet cases.
- For weaker cases, the flow becomes transitional.
- Would like to understand **the point of switching** between laminar and turbulent buffet.



Influence of forcing amplitude

