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STUDY ON THE ORBITAL MANEUVERING CAPABILITY OF H-2A KICK STAGE

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This paper describes a concept study of an optional kick stage system named "PLUS (for Planetary mission, Long-duration small-thrust Upper Stage)" equipped with a relatively small-thrust engine for interplanetary missions. The thrust force of PLUS assumed in this study is a maximum 29.4 kN, which is relatively small, used to inject a payload into interplanetary orbit with sufficiently low gravity loss i.e. less than 2 %, although two split delta-Vs such as the Russian Proton/Breeze-M will improve performance efficiency¹. The orbital maneuvering capability of PLUS system is evaluated through Mars orbital maneuvering simulations. In this study, two types of PLUS systems are assumed: First, a 29.4 kN thrust force kicks stage system designated as "PLUS1" to inject the 3000 kg main payload into Mars transfer orbit. Second, a 9.8 kN thrust force small PLUS system designated as "PLUS2" to inject a 500 kg secondary payload into Mars transfer orbit. In the first case, the above-mentioned split delta-Vs are conducted to inject the main payload into Mars transfer orbit with sufficiently low gravity loss. In the second case, on the other hand, PLUS2 attached to the secondary payload is dual launched together with a primary payload into a geostationary transfer orbit, GTO, whereupon PLUS2 is initiated slightly before perigee to inject the secondary payload into Mars transfer orbit utilizing Electric delta-V Earth Gravity Assist, EDVEGA scheme via the on-board Ion Electric propulsion System, IES^{2, 3}. Throughout the simulations, some optimized configurations of PLUS system covering a wide variety of space missions are suggested in this paper.

I. INTRODUCTION

The main purpose of this study is to evaluate the launch capability of an optional kick stage system named "PLUS (for Planetary mission, Long-duration small-thrust Upper Stage)" equipped with a LOX/ethanol engine, which is under development in the Kakuda space center of the Japan Aerospace Exploration Agency, JAXA, from an interplanetary mission i.e. Mars mission perspective.



Figure 1. Launch System Configuration of Case 1

In this study, two different types of PLUS systems are assumed: First, a 29.4 kN thrust force kick stage system designated as "PLUS1" to inject a 3000 kg main payload into Mars transfer orbit. Second, a 9.8 kN thrust force small PLUS system designated as "PLUS2" to inject a 500 kg secondary payload into Mars transfer orbit.

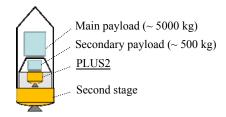


Figure 2. Launch System Configuration of Case 2

In the first case, designated as "Case 1" in this study, PLUS1 is assumed to be optionally attached to the Japanese flagship launch system, H-2A. Figure 1 shows the launch system configuration of "Case 1". In this case, the main payload and PLUS1 are injected into a 300 km altitude circular parking orbit via the first and second stages of H-2A, whereupon PLUS1 is fired to inject the main payload into Mars transfer orbit. However, since the thrust force of the assumed PLUS1 is relatively small for such use, two split delta-Vs, such as the Russian Proton/Breeze-M, are applied to improve

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the performance efficiency of the above-mentioned PLUS1 system. Gravity loss is focused on to measure the performance efficiency of the low-cost and smallthrust PLUS system.

In the second case, designated as "Case 2", PLUS2 attached to the secondary payload is dual launched together with a primary payload into a geostationary transfer orbit, GTO, whereupon PLUS2 is initiated at perigee to inject the secondary payload into the energy garnering orbit, EGO. Figure 2 shows the launch system configuration of Case 2.

Although the relative velocity at Earth departure is almost zero, the on-board IES accelerates the spacecraft through the EDVEGA scheme, which increases the Earth relative velocity at the Earth re-encounter point up to about 2.7 km/sec; enabling the spacecraft to inject into Mars transfer orbit after the Earth gravity assist.

Throughout the simulations, some optimized configurations of PLUS system covering a wide variety of space missions are suggested in this paper.

II. FORCE MODEL AND LAUNCH WINDOW

II.I Force Model

In this study, the gravitational forces of the Sun and Earth are considered. It is assumed that the orbits of the Earth and the destination planet i.e. Mars lie on the ecliptic plane. Conversely, the eccentricities of both orbits are considered.

II.II Launch Window

The transfer orbit between the Earth and Mars is determined by solving Lambert's problem. The outbound relative velocity at the Earth departure, designated as V_{∞} , is also determined by the transfer orbit. In practice, the ΔV generated by a launch vehicle is limited and the lower ΔV the better.

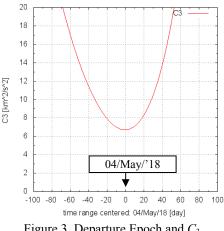


Figure 3. Departure Epoch and C_3

In this study, May 4th, 2018 is determined as the departure epoch to Mars. Figure 3 shows the

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relationship between the launch epoch and orbital energy C_3 , which is the square of the out-bound relative velocity at the Earth departure. The time of flight for the transfer is 200 days.

III. ORBITAL MANEUVER

III.I Orbital Maneuver of Case 1

In Case 1, the main payload and PLUS1 are initially injected into a 300 km altitude circular parking orbit. The PLUS1 is initiated at the optimal point to inject the payload into Mars transfer orbit.

Generally, a kick stage is fired only once, designated as "1-Burn" in this paper, and the spacecraft is injected into the transfer orbit. However the thrust force assumed in this study is relatively small i.e. 29.4 kN, hence split delta-Vs, designated as "2-Burn", are applied and the performance efficiency, i.e. gravity losses of both cases, are compared. Figure 4 shows the orbital maneuvers in the cases of "1-Burn" and "2-Burn".

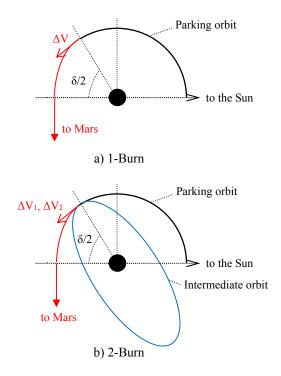


Figure 4. Diagram of Orbital Maneuver of Case 1

The angle $\delta/2$, which is the angle between the "impulsive" ΔV start point and the Sun-Earth line, is described as the following equation:

$$\sin\!\left(\frac{\delta}{2}\right) = \frac{1}{1+\Psi} \tag{1}$$

where;

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$$\Psi \equiv \left(\frac{V_{\infty}}{V_p}\right)^2 \tag{2}$$

 V_{∞} is the out-bound Earth relative velocity to Mars, which is determined by Lambert's theorem, and V_p is the orbital velocity of 300 km altitude circular parking orbit. In this study, the value of V_{∞} is 2.6 km/s and V_p is 7.7 km/s, hence the turning angle $\delta/2$ is 64.0 deg.

The main purpose of the Case 1 study is to evaluate the gravity loss of PLUS1, hence finite time thrust is simulated. Figure 5 shows a diagram of the finite thrust simulation.

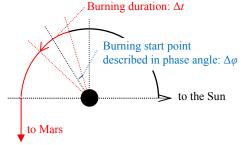


Figure 5. Diagram of Finite Time Thrust

Here, the mass of propellant m_p [kg] consumed in the burning duration, is described in the following;

$$m_p = |\dot{m}| \Delta t \tag{3}$$

where \dot{m} [kg/sec] is the mass flow rate which is defined as:

$$\left|\dot{m}\right| = \frac{F}{gI_{sp}} \tag{4}$$

where F [N] is the thrust force, g is the standard Earth's gravitational acceleration i.e. 9.80665 m/sec², and I_{sp} [sec] is the specific impulse.

The velocity change, ΔV , produced by the propellant m_p is described as the rocket equation⁹;

$$\Delta V = gI_{sp} \ln \left(\frac{m_0}{m_0 - m_p} \right) \tag{5}$$

where m_0 [kg] is the initial mass of PLUS system including the payload. From Eqs. (5), m_p is also described as the follows;

$$m_{p} = m_{0} \left(1 - \exp\left(-\frac{\Delta V_{esc}}{gI_{sp}}\right) \right)$$
(6)

where ΔV_{esc} [m/s] is the ΔV required to inject the spacecraft into Mars transfer orbit from the parking orbit. ΔV_{esc} is described as the following;

$$\Delta V_{esc} = \sqrt{V_{\infty}^2 + \frac{2\mu_E}{r_p}} - \sqrt{\frac{\mu_E}{r_p}}$$
(7)

where μ_E is the Earth's gravitational constant 3.986004418×10¹⁴ m³/sec² and r_p [m] is the radius of the parking orbit. As mentioned, V_{esc} [m/s] is determined by solving Lambert's problem.

From the Eqs. (3), Eqs. (4) and Eqs. (6) then the burning duration Δt is described as the following:

$$\Delta t = \frac{m_0}{F} g I_{sp} \left(1 - \exp\left(-\frac{\Delta V_{esc}}{g I_{sp}}\right) \right)$$
(8)

The burning start point is described in phase angle $\Delta \varphi$. The ΔV starts at the point angle $\Delta \varphi$ earlier from the impulsive ΔV point. The phase angle $\Delta \varphi$ is described in the following:

$$\Delta \varphi = \frac{\Delta t}{2} \sqrt{\frac{\mu_E}{a^3}} \tag{9}$$

where *a* [m] is the semi-major axis of the orbit i.e. the "circular" parking orbit, or "highly elliptical" intermediate orbit.

III.II Orbital Maneuver of Case 2

In Case 2, the primary payload and secondary payload attached to PLUS2 are dual launched into GTO. The launch epoch and apsis line of the GTO are determined by the mission requirement of the primary payload rather than secondary payload.

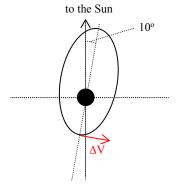


Figure 6. Initial GTO

In this study, the GTO into which the Wideband Inter-Networking engineering test and Demonstration Satellite, WINDS of JAXA, has been injected, is

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assumed to be the initial GTO of the primary payload. The PLUS2 is initiated slightly before perigee to inject the secondary payload into EGO. The departure C_3 is almost zero. Figure 6 shows the initial GTO in this study.

During the EGO flight, the on-board IES accelerates the spacecraft. The relative velocity at the Earth reencounter increases up to about 2.7 km/sec after 1.3 year EGO flight. Figure 7 shows the EDVEGA trajectory in the inertial frame.

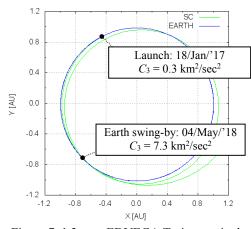


Figure 7. 1.3 year EDVEGA Trajectory in the Heliocentric Inertial Frame

Table 1 shows the specification of the on-board IES, which is almost equivalent to the IES of HAYABUSA-2 of JAXA⁶.

Table 1. Specification of IES of Cases 2		
Terms	Unit	Values
I_{sp}	sec	3000
\dot{F}	mN	30

The specific impulse, I_{sp} and thrust force, F, change depending on the heliocentric distance of the spacecraft designated as R.

Here, we assume that the thrust force F and the specific impulse I_{sp} are proportional to the generated power P as the following¹¹;

$$F = k_1 P^{\alpha} \tag{10}$$

$$I_{sp} = k_2 P^{\beta} \tag{11}$$

where k_1 and k_2 are constants and α and β are parameters. On the other hand, it is approximated that the power *P* is proportional to the product of *F* and I_{sp} as the following;

$$P = k_3 F \cdot I_{sp} = k_1 k_2 k_3 P^{\alpha + \beta} \tag{12}$$

where k_3 is constant. Consequently, the following relationship is revealed;

$$\beta = 1 - \alpha \tag{13}$$

When we describe the generated power at 1 AU as P_1 , the following relationship is derived;

$$\frac{P}{P_1} = \left(\frac{1AU}{R}\right)^2 \tag{14}$$

From Eqs. (10), Eqs. (11), Eqs. (13) and Eqs. (14), the following equations are derived;

$$\frac{F}{F_1} = \left(\frac{P}{P_1}\right)^{\alpha} = \left(\frac{1AU}{R}\right)^{2\alpha}$$
(15)

$$\frac{I_{sp}}{I_{sp1}} = \left(\frac{P}{P_1}\right)^{1-\alpha} = \left(\frac{1AU}{R}\right)^{2-2\alpha}$$
(16)

where F_1 , I_{sp1} are the thrust force and specific impulse at 1 AU, respectively. In this study, the parameter α is set to be 0.5¹¹. Consequently, the following equation is derived;

$$\frac{I_{sp}}{I_{sp1}} = \frac{F}{F_1} = \frac{1AU}{R}$$
(17)

IV. METHOD OF ANALYSIS

IV.I Analysis of Case 1

To evaluate and compare the gravity losses of "1-Burn" and "2-Burn", the optimal burning duration and burning start point must be determined. For this purpose, Sequential Quadratic Programming, SQP, method is used in this study^{7, 8}. At first, the SQP algorithm for "1-Burn" simulation is described as the following:

 $\frac{\text{SQP algorithm (1-Burn)}}{1) \text{ Control parameters}}$ $\Delta t, \Delta \varphi, \tau$

2) Equality constraint
$$r_{SC} = r_M$$
 at arrival epoch

3) Inequality constraint
$$\Delta t > 0.0, \tau > 0.0$$

4) Objective function minimize m_p

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where, τ is the time of flight from the Earth to Mars, *rsc* and *r_M* are the 2-dimensional position vectors of the spacecraft and the Mars in the heliocentric reference frame, respectively. The total ΔV of the finite time thrust, designated as ΔV_{finite} is described as the follows from Eqs. (3) and Eqs. (5):

$$\Delta V_{finite} = g I_{sp} \ln \left(\frac{m_0}{m_0 - |\dot{m}| \Delta t} \right)$$
(18)

The gravity loss of the finite time thrust is defined as follows⁴:

gravity loss
$$\approx \frac{\Delta V_{finite}}{\Delta V_{impulse}} - 1$$
 (19)

where the $\Delta V_{impulse}$ is computed by Eq. (7) and the initial Δt and $\Delta \varphi$ are determined by Eqs. (8) and (9). The initial τ is 200 days.

On the other hand, the SQP algorithm for "2-Burn" simulation is the following:

 $\frac{\text{SQP algorithm (2-Burn)}}{1) \text{ Control parameters}} \\ \Delta t_1, \Delta t_2, \Delta \varphi_1, \Delta \varphi_2, \tau$

- 2) Equality constraint $r_{SC} = r_M$ at arrival epoch
- 3) Inequality constraint $\Delta t_1 > 0.0, \Delta t_2 > 0.0, \tau > 0.0$

4) Objective function minimize total m_p

where the subscript numbers correspond to ΔV_1 or ΔV_2 .

IV.II Analysis of Case 2

In the Case 2 study, the optimal EGO is computed by minimizing the departure ΔV which is applied at the perigee point of the initial GTO. For this simulation, an initial EGO is determined in advance through heuristic approach by changing the time of flight during the EGO phase τ_{EGO} , ΔV at perigee ΔV_p , IES throttle level *TL*, and IES thrust unit vector, *F*_{IES}. $V_{\infty O}$ at the Earth reencounter is also determined from the trajectory design between the Earth and Mars. Once the initial trajectory is determined, the EGO is divided into 48 nodes, and the parameters are input to the following SQP method:

SQP algorithm (Case 2) 1) Control parameters $\Delta V_{p}, \tau_{EGO}, TL_{n}, F_{IESn}$

2) Equality constraint

 $R_{SC-E} = R_{SOI}$ at Earth re-encounter $|V_{\infty I}| = |V_{\infty O}|$ at Earth re-encounter

3) Inequality constraint

$$0.0 \le TL_n \le 1.0$$

 $200 \text{ (km)} \le Alt_{sb}$

4) Objective function
minimize
$$\Delta V_p$$

where R_{SC-E} is the range between the spacecraft and the Earth at the Earth re-encounter, R_{SOI} is the radius of the sphere of influence of the Earth, $V_{\infty I}$ and $V_{\infty O}$ are the inbound and out-bound relative velocities at the Earth re-encounter, and Alt_{sb} is the altitude at the Earth swing-by. The subscript *n* attached to *TL* and *F*_{IES} is the node number.

The radius of the Earth's sphere of influence, R_{SOI} , is described as follows⁵:

$$R_{SOI} = \left(\frac{M_E}{M_S}\right)^{\frac{2}{5}} A_E \tag{20}$$

where M_E and M_S are the mass of the Earth and Sun, respectively, and A_E is the heliocentric distance of the Earth.

When the turning angle Φ , which is the angle between $V_{\infty I}$ and $V_{\infty O}$ at the Earth swing-by are known, the range between the Earth and spacecraft at the Earth swing-by, r_{SC-E} , is described as follows^{3, 5};

$$r_{SC-E} = -\frac{\mu_E}{V_{\infty}^2} \left(1 + \frac{1}{\cos f_{\infty}} \right)$$
(21)

where;

$$\Phi = 2f_{\infty} - \pi \tag{22}$$

The Alt_{sb} is determined by subtracting the Earth's radius from r_{SC-E} .

Note that the on-board IES is initiated 3 days after launch. Besides, the IES is activated during only EGO phase i.e. the IES is not used during and after the Earth swing-by.

V. RESULTS OF ANALYSIS

V.I Results of Case 1 Analysis

Table 2 summarizes the specification of PLUS1 of Case 1. m_s is the mass of PLUS1 structure, m_p is the propellant mass, m_{pl} is the payload mass, η is the propellant mass fraction, and F is the thrust force of PLUS1.

 Table 2. Specification of PLUS1 of Case 1

Terms	Unit	Values
m_0	kg	17363
m_s	kg kg	1867
m_p	kg	12496
m_{pl}	kg	3000
η		0.87
I_{sp} F	sec	340
F	kN	29.4

Table 3 summarizes the keplerian elements at the initial epoch i.e. 00:00, May, 4th, 2018 (UTC). In this analysis, the parking orbit lies on the ecliptic plane i.e. the inclination is 23.4 deg. In Table 3, *a* is the semimajor axis, *e* is the eccentricity, *i* is the inclination, Ω is the right ascension of the ascending node, ω is the argument of perigee and *v* is the true anomaly. Note that the Sun-Earth line is inclined 40 deg from the +X direction of the heliocentric reference frame at the initial epoch. The simulation starts from the Sun-Earth line, hence the true anomaly *v* at the initial epoch is 40 deg.

Table 3. Keplerian Elements of Parking Orbit at Initial Epoch

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Term	Unit	Values
а	km	6678.0
е		0.0
i	deg	23.4
Ω	deg	0.0
ω	deg	0.0
v	deg	40.0

The results of Case 1 analysis are summarized in Table 4.

Table 4. Results of Case 1 Analysis			
Term	Unit	1-Burn	2-Burn
$\Delta V_{impulse}$	km/s	3.505	3.503
ΔV_{finite}	km/s	3.662	3.547
$\Delta \varphi_1$	deg	42.1	26.4
$\Delta \varphi_2$	deg		5.6
Δt_1	sec	1311.6	808.8
Δt_2	sec		480.1
τ	day	196	191
residual m_p	kg	923	1125
gravity loss	%	4.480	1.256

From the results of Table 4, the gravity loss apparently improves by applying the 2-Burn method. The difference in residual mass of the propellant between 1-Burn and 2-Burn is about 200 kg.

As mentioned, from a gravity loss perspective, the "2-Burn" case is superior, however, in the "2-Burn" case, PLUS1 is additionally required to reignite after one revolution in the intermediate orbit i.e. 4.3 hours.

Table 5. shows the keplerian elements at the ΔV_2 burning start point.

Table 5. Keplerian Elements of Intermediate Orbit at
ΔV_2 Burning Start Point

ΔV_2 building Start Point		
Term	Unit	Values
a	km	13418.3
е		0.5
i	deg	23.4
Ω	deg	0.0
ω	deg	157.5
v	deg	341.5
orbital period	hr	4.3

Note that the argument of perigee ω is 157.5 which is 117.5 deg from the Sun-Earth line. Thus the angle $\delta/2$ is 62.5 deg which is almost equivalent to the value computed by Eqs. 1 i.e. 64.0 deg (See Figure 4).

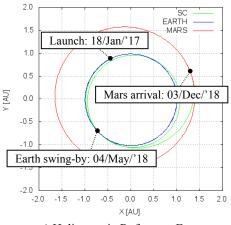
V.II Results of Case 2 Analysis

Table 6 summarizes the specification of the PLUS2 of Case 2.

Table 6. Specification of PLUS	2 of Case 2
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Terms	Unit	Values
m_0	kg	800
m_s	kg	90
m_p	kg kg	210
m_{pl}	kg	500
η		0.7
I_{sp}	sec	340
\dot{F}	kN	9.8

The H-2A 204 has the ability to launch a 6000 kg payload into GTO. Accordingly, if the mass of the primary payload is less than 5000 kg, an 800 kg secondary payload, consisting of a 500 kg small explorer and a 300 kg PLUS2, can be launched together with the primary payload.



a) Heliocentric Reference Frame

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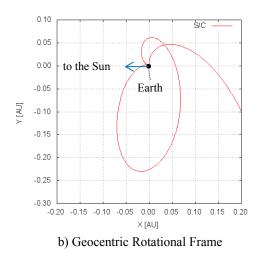


Figure 8. EDVEGA and Mars Transfer Trajectory

Figure 8 shows the EDVEGA and Mars transfer trajectory optimized by the SQP algorithm in the heliocentric reference frame and geocentric rotational frame.

Table 7 summarizes the result of Case 2 analysis. Based on the results summarized in Table 7, PLUS2 system assumed as shown in Table 6 does work for the secondary payload injection into EGO from the initial GTO.

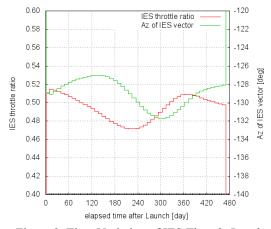


Figure 9. Time Variation of IES Throttle Level and Thrust Vector

Figure 9 shows the time variation of IES throttle level and IES thrust vector in the heliocentric reference frame. As shown in the figure, the IES thrust vector is

almost constant in the heliocentric reference frame during the EGO phase. The mass of propellant consumed by the IES is 41.2 kg while the propellant of HAYABUSA is 66 kg^{12} .

Table 7. Results of Case 2 Analysis		
Terms	Unit	Values
ΔV_p	m/s	796.8
Δt	sec	57.9
m_p consumed	kg	170
$ au_{EGO}$	day	470

Launch Window Expansion

In the type of use of Case 2, the secondary payload cannot choose the "desired" launch epoch. The launch windows of deep-space missions are generally narrow i.e. 1~2 weeks, hence a method of expanding the launch window of the secondary payload i.e. small explorer is necessary for the Case 2 use. The study on the flexible orbit design technique which enables "any-time" launch of the deep-space explorer is under way. According to the results of the preliminary study, the launch window can be drastically widened i.e. 360 days¹⁰.

VI. CONCLUSION

This study assessed the launch capability of the optional kick stage, PLUS (for Planetary, Long-duration Upper Stage) system through numerical simulations.

In Case 1 study, it was assumed to launch a 3000 kg explorer to Mars by PLUS system designated as "PLUS1". The thrust force of PLUS1 is relatively small i.e. 29.4 kN however split ΔVs improved the performance efficiency to practical level i.e. 1.3 % gravity loss, while the loss of "1-Burn" case is 4.5 %. This improvement means about 200 kg propellant is saved by the split ΔVs , although PLUS1 is required to reignite at 4.3 hours after the first ΔV .

In Case 2 study, on the other hand, it was assumed that the secondary payload consisting of a 500 kg explorer and small PLUS system, designated as "PLUS2", is dual launched into GTO together with a 5000 kg primary payload. On the perigee point of the GTO, PLUS2 is ignited to inject the explorer into the trajectory whose orbital energy, C_3 , is almost zero. After the injection, the explorer voyages to Mars through EDVEGA scheme via the on-board IES. The numerical simulation revealed a HAYABUSA class explorer can be launched as a secondary payload into GTO, and also the explorer can reach Mars after 1.3 year energy garnering phase.

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