

Verification and Validation of Turbulence Models

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Outline

- Introduction to RANS and V&V
- Overview of some past turbulence-modelingrelated workshops
 - ERCOFTAC SIG 15
 - CFD Uncertainty Analysis
 - CFDVAL2004
 - DPW and HiLiftPW
- NASA Turbulence Modeling Resource Website
 - Its purpose and status
- Summary

Reynolds-Averaged Navier-Stokes (RANS)

- RANS is currently the bread-and-butter of the aerospace industry
 - Useful for analysis & design
 - Complex cases can be run in reasonable turn-around times on today's computers
 - Weak link: the RANS turbulence models required to close the equations have some severe limitations
- Scale-resolving methods are typically more accurate than RANS, but are currently too expensive for routine use on complex configurations at high Reynolds numbers
 - Large eddy simulation (LES), Direct numerical simulation (DNS), and hybrid RANS-LES
 - Seen as the future, but when will computers be powerful enough to make these calculations routine?*

*Also, Moore's Law appears to be losing traction! 3



Focus of this talk is on RANS





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Verification & Validation (V&V)

• Verification:

 Software implementation accurately represents developer's description of the model

Validation:

 Determination of degree to which model accurately represents the real world (keeping in mind intended use)



Verification:

 Software implementation accurately represents developer's description of the model

NO BUGS; coded correctly

- Validation:
 - Determination of degree to which model accurately represents the real world (keeping in mind intended use)



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NASA

Can RANS results be trusted?

- RANS is considered trustworthy for many attached flow aerodynamic applications
- RANS is not trusted for aerodynamic separated flows
- In an effort to document/improve RANS capabilities, many <u>validation</u> workshops have been held
 - Some to be discussed here
- But without <u>verification</u>, it is often difficult to draw firm conclusions from validation exercises when codes do not agree



Example from Drag Prediction Workshop 3 (DPW-3)

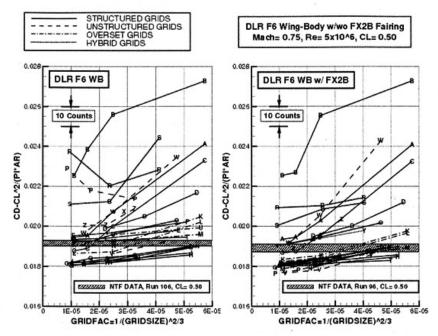


Figure from Vassberg et al., AIAA Paper 2008-6918, August 2008

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How easy is it to code a turbulence model as intended?

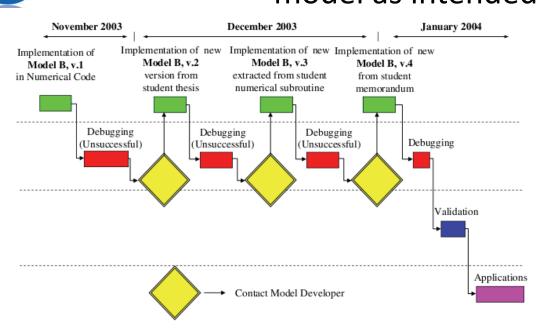


Figure from Computers & Fluids 36 (2007) 1373-1383



What is needed?

- Verification:
 - Method of Manufactured Solutions (MMS), e.g., Roy et al.
 - Compare against known analytic solutions
 - Grid convergence studies and comparison with other verified codes for benchmark problems
- <u>Validation</u> typically involves comparison against experiment, DNS, or LES
 - Care must be taken :
 - To understand the error in the experiment, DNS, or LES
 - To get the BCs and geometry right in the RANS (apples to apples)
 - To reduce discretization error and iterative convergence error in the RANS

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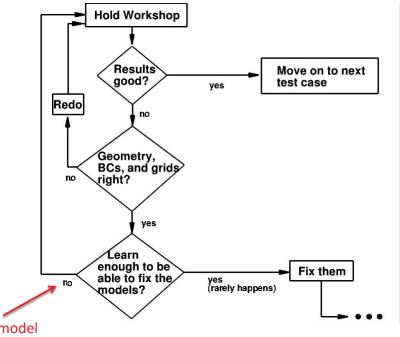
rarely done

- <u>Validation</u> typically involves comparison against experiment, DNS, or LES
 - Care must be taken :
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Turbulence Modeling Workshops

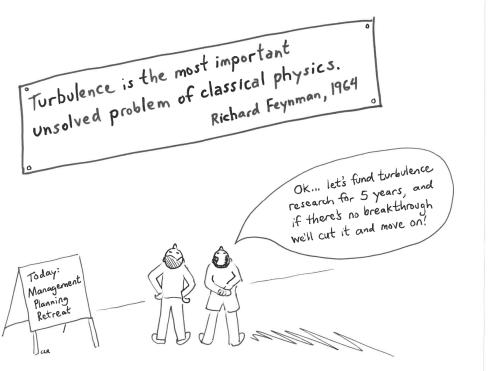


...because model results are all over the map!

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Where does this leave us?





Summary of some past workshops (related to turbulence modeling)

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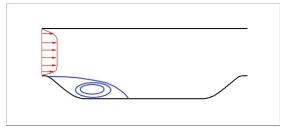
ERCOFTAC SIG 15

- Special interest group on "refined turbulence modeling"
 - 14 workshops since early 1990s
 - Recently have started to include eddy-resolving methods (e.g., LES, hybrid RANS-LES)
 - Some major conclusions:
 - RANS predicts 2-D separated hill flows poorly

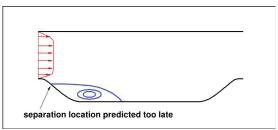


Hill-type separated flows

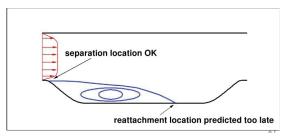
Correct result



Incorrect result typical with k-epsilon



Incorrect result typical with SA, SST, k-omega





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 - Complex cases (e.g., flow inside curved duct, jet impinging on rotating disk, 3-D separated diffuser) tend to be predicted by EASMs and RSMs better than linear models

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 - RANS predicts 2-D separated hill flows poorly
 - Complex cases (e.g., flow inside curved duct, jet impinging on rotating disk, 3-D separated diffuser) tend to be predicted by EASMs and RSMs better than linear models
 - Different codes with same turbulence models often obtain very different results – REASONS UNKNOWN



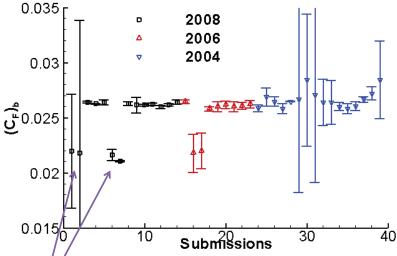
CFD Uncertainty Analysis

- Series of 3 workshops held in Lisbon during 2000s
- Focus on uncertainty estimators, such as Roache's Grid Convergence Index (GCI)
- 2-D hill and 2-D backward facing step
- Progressive improvement seen:
 - 1st workshop: possibility of undetected coding errors
 - 2nd workshop: prescribed use of MMS
 - 3rd workshop: included MMS, grid convergence, and uncertainty estimates for both CFD and experiment

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MMS: led to more consistency for backward facing step

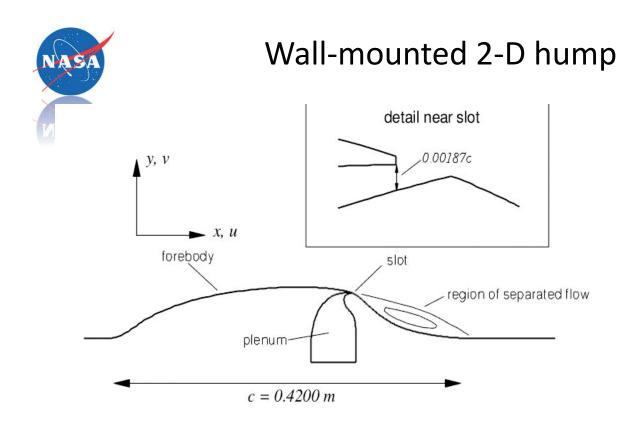


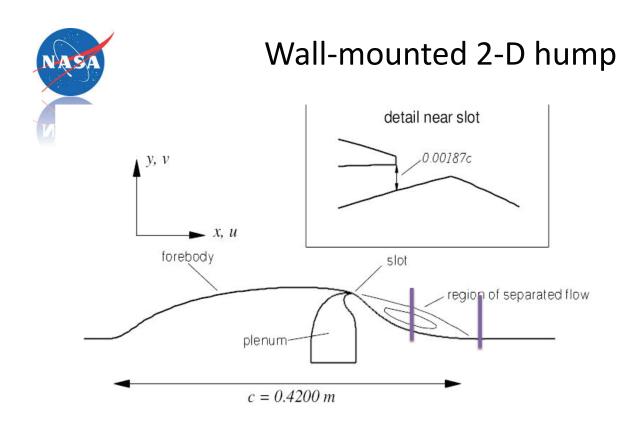
Two outliers in 2008: one used much coarser grid than everyone else, the other did not perform code verification (MMS) exercise

Figure from AIAA 2009-3647



- Workshop focused on synthetic jets and turbulent separation control
- Three cases:
 - Case 1: 2-D synthetic jet into quiescent air
 - Case 2: circular synthetic jet in crossflow
 - Case 3: 2-D flow over wall mounted hump (no flow control, steady suction, and synthetic jet)
- Major conclusions:
 - Difficulty measuring time-dependent BCs in experiment
 - Inconsistent application of BCs in CFD
 - Case 3 provided clear evidence of RANS deficiencies
 - Use of website to post data, grids, etc. promoted wide use (over 40 subsequent papers on Case 3 alone)





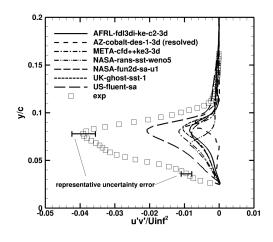
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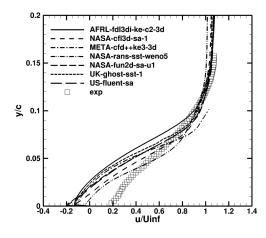


Hump flow predictions by RANS

Inside bubble

Downstream of exp reattachment





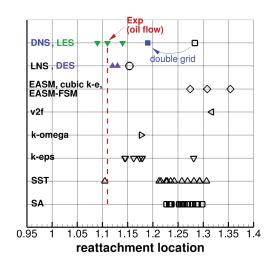
Turbulent shear stress magnitude in separated shear layer severely under-predicted by RANS. Consequently too little turbulent mixing; reattachment & recovery comes too late.

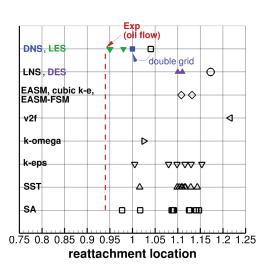


Scale-resolving methods can do better (but not always*)

No flow control

Steady suction flow control





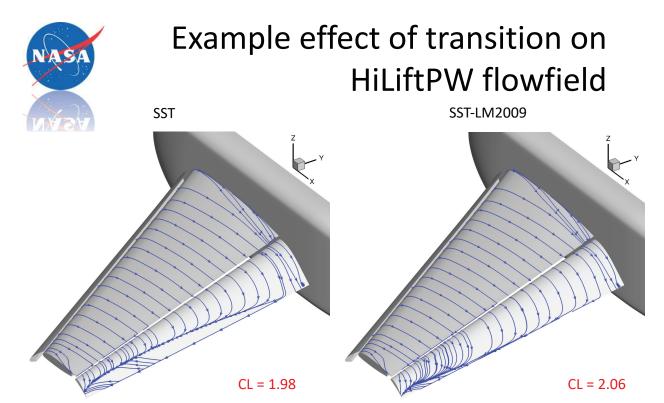
* Considerable expertise seems to be required to perform scale-resolving simulations correctly!

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DPW and HiLiftPW

- Focus on drag prediction and high lift prediction for aircraft configurations
 - Most participants have used SA or SST turbulence models
 - Lack of consistency between codes using the same model
 - DPW:
 - A big issue has been wing-root separation bubble
 - Strongly a function of grid size, grid topology, numerical method, and turbulence model
 - HiLiftPW:
 - SA-based models generally agree better with experiment
 - But transition is typically not accounted for



When you account for transition, SST results improve dramatically

Experimental C_L = 2.05 @ alpha=13 deg.

But this does not explain why "fully turbulent" SA model also yields good C_L results

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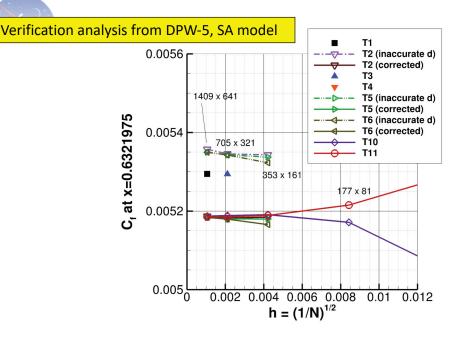


Turbulence Modeling Resource (TMR) Website

- Established in late 2000s by NASA in collaboration with AIAA Turbulence Model Benchmarking Working Group (TMBWG)
- Goals:
 - Provide accurate and up-to-date information on widely-used RANS turbulence models, <u>including model naming conventions</u>
 - Help verify that turbulence models are implemented correctly (as intended)
 - Compare model predictions for fundamental flow problems
 - Serve as forum for helping to disseminate new models
 - Provide some additional resources:
 - Experimental, DNS, and LES databases (incl data from "Stanford Olympics", Bradshaw et al.)
 - · MMS resources and information
 - Convergence properties, numerics, etc.



How has the NASA TMR website been useful?



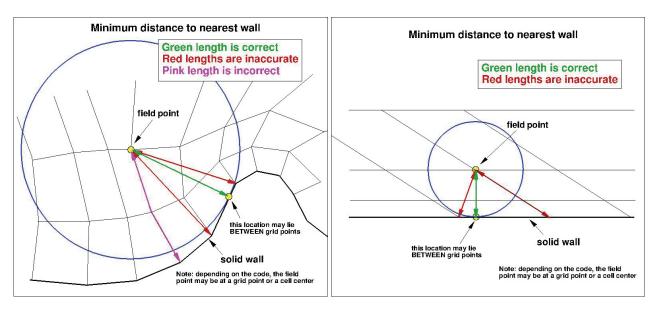
T2, T5, and T6 found to be inaccurate due to use of approximate minimum distance function

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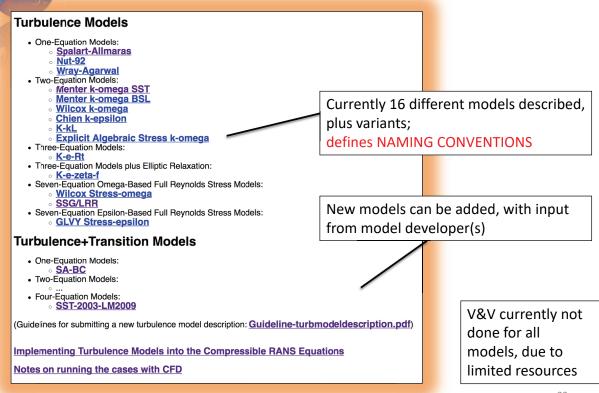
Distance function

- Used by SA, SST, other models
- If not done accurately, results can be inconsistent (grid-dependent)





Description of Turbulence Models





Verification Cases

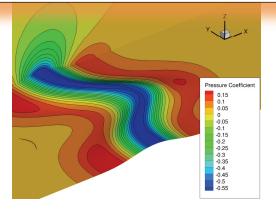
Implementing Turbulence Models into the Compressible RANS Equations Notes on running the cases with CFD

Turbulence Model Verification Cases and Grids

VERIF/2DZP: 2D Zero pressure gradient flat plate

VERIF/2DZF. 2D 2cl o places
VERIF/2DCJ: 2D Coflowing jet
VERIF/2DB: 2D Bump-in-channel
VERIF/2DANW: 2D Airfoil Near-Wake
VERIF/3DB: 3D Bump-in-channel

Website began with 4 cases; the VERIF/2DANW case has been recently added

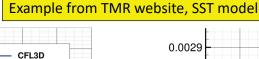


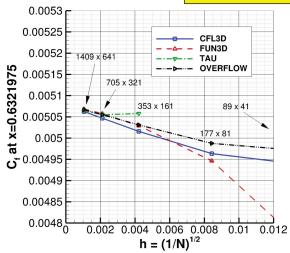
All grids are provided

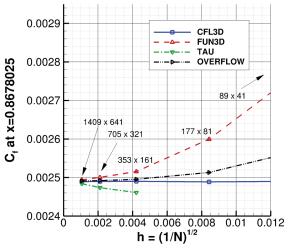
3-D Bump-in-channel verification example, using Wilcox2006 model

"Verification via Comparison"

 Use grid-convergence studies and comparison with other verified codes for benchmark problems







Many more details available on website

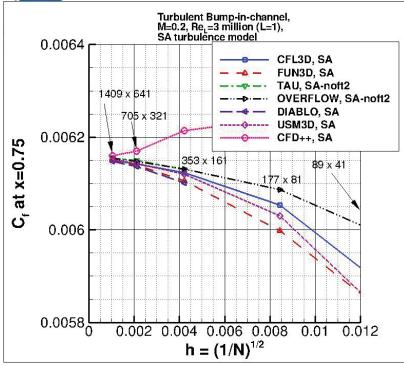


Verification Cases

- "Verification by comparison" is not fool-proof
 - Sufficient iterative convergence is very important!
 - 2 (or more) codes may have similar errors, or particular errors may not show up for the cases considered
 - But the more codes that agree, and the more cases we do, the more confidence we have
 - Transparency and openness of TMR allows the whole world to check its accuracy (and tell us if a problem or inconsistency is found)
- Model Readiness Rating (MRR) system
 - 0=no results yet; model description only
 - 1=model only in one code on TMR
 - 2=two or more codes agree on at least two cases on TMR
 - 3=two or more codes from different organizations agree on TMR (independently obtained)
 - 4=turbulence model underwent Method of Manufactured Solutions in at least 1 code



Verification Cases



Example of a turbulence model (SA) with MRR Level=4

We have very high confidence in the SA results on the TMR – users can trust these results

Other models with MRR Level=3 or 4 currently:

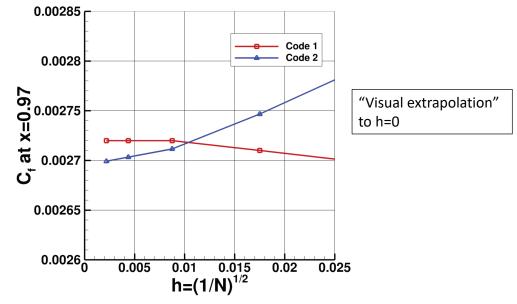
- -SA
- -SA-RC
- -SST
- -SST-V
- -SSG/LRR-RSM-w2012
- -K-kL-MEAH2015

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Verification Cases

Example of a turbulence model NOT posted, because "verification by comparison" has not yet been successfully achieved





Validation Cases

Turbulence Model Validation Cases and Grids

. Basic Cases:

o 2DZP: 2D Zero pressure gradient flat plate

2DML: <u>2D Mixing Layer</u>

2DANW: 2D Airfoil near-wake
 2DN00: 2D NACA 0012 airfoil

ASJ: Axisymmetric Subsonic jet

AHSJ: Axisymmetric Hot subsonic jet

ANSJ: Axisymmetric Near-sonic jet

o ASBL: Axisymmetric Separated boundary layer

o ATB: Axisymmetric Transonic Bump

9 "basic" cases and 9 "extended" cases, as determined by the TMBWG

committee

• Extended Cases:

o 2DZPH: 2D Zero pressure gradient high Mach number flat plate

o 2DBFS: 2D Backward facing step

o 2DN44: 2D NACA 4412 airfoil trailing edge separation

o 2DCC: 2D Convex curvature boundary layer

o 2DWMH: 2D NASA wall-mounted hump separated flow

o ASWBLI: Axisymmetric Shock Wave Boundary Layer Interaction near M=7

ACSSJ: Axisymmetric Cold Supersonic Jet
 AHSSJ: Axisymmetric Hot Supersonic Jet

o 3DSSD: 3D Supersonic square duct

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Validation Cases

		Free shear flows			Wall flows		P- grad- ients	Curv- ature	Compressibility			Secon- dary flows	Turb Heat Flux	Higher Mach	Vortex flows	Shock	Separ- ation
		Jet Anom- aly	Mixing layer	Wakes	of	Law of wake			Mixing	Van Driest I	Van Driest II						
Boundary layers	2DZP*				Υ	Υ											
	2DZPH									Υ	Υ		Υ	Υ			
	ASBL*				Υ		weak										weak
Mixing layer/ wakes	2DML*		Υ														
	2DANW*			Υ													
Jets	ASJ*	Υ															
	ANSJ*	Υ							Υ					Υ			
	AHSJ*	Υ											Υ				
	ACSSJ*	Υ							Υ					Υ			
	AHSSJ*	Υ							Υ				Υ	Υ			
Airfoils	2DN00*						Υ										weak
	2DN44						Υ										Υ
Bump flows	ATB*						Υ							Υ		Y	Y
	2DWMH						Υ										Y
Shock/boundary layer interaction flows	ASWBLI						Y						Υ	Y		Y	Y
Internal flows	2DCC						Υ	Υ									
	2DBFS						strong										Υ
	3DSSD						Υ					Υ	Υ	Υ			

(* indicates "Basic Case")



Other Aspects of TMR

- **Databases**
- Manufactured Solutions
- **Numerical Analysis**

Turbulent Flow Validation Databases

The data in the following links are publicly available and are provided here as a convenience. They are provided as-is and accuracy is not guaranteed; questions should be dithe sources of the data provided.

- Data from "Collaborative Testing of Turbulence Models"
 Data from Other Experiments
- Data from Other Direct Numerical Simulations (DNS)
 Data from Other Large Eddy Simulations (LES)

Turbulent Manufactured Solutions

• Information from Lisbon "Workshop on CFD Uncertainty Analysis" series

Cases and Grids for Turbulence Model Numerical Analysis

- 2D Finite Flat Plate
 2D NACA 0012 Airfoil
 2D Hemisphere Cylinder
 3D Modified Bump
 3D Modified Supersonic Square Duct
 3D Hemisphere Cylinder (old)
 3D Hemisphere Cylinder (new)
 3D ONERA M6 Wing

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Data from "Collaborative Testing"

- From Bradshaw et al. (used with permission)
- Includes data from "Stanford Olympics"

Incompressible Flow Cases from 1980-81 Data Library

This grouping contains the incompressible-flow cases from the 1980-81 Data Library. The data in the original files are in normalized format, as explained on p. 60 of the 1980-81 Proceedings ("The 1980-81 AFOSR-HTTM Stanford Conference on Complex Turbulent Flows: A Comparison of Computation and Experiment, Volumes I, II, and III, edited by S. J. Kline, B. J. Cantwell, and G. M. Lilley, Stanford University, 1981). The 1980-81 Conference Proceedings also give a full description of the cases. (These cases comprise the contents of the original disk "d1", with the exception of 0411 (Cantwell Cylinder), 0441 (Wadcock airfoil), 0511 (Shabaka wing-body junction), 0512 (Humphrey bend), which were too large to fit on the original disk.)

- Case F-0111: Developing Flow in a Square Duct (Po et al)
 Case F-0112: Secondary Currents in the Turbulent Flow Through a Straight Conduit (Hinze)
 Case F-0141: Increasingly Adverse Pressure Gradient Flow (Samuel and Joubert)
 Case F-0142: Six-Degree Conical Diffuser Flow, Low and High Core Turbulence (Pozzorini)
 Case F-0211: Effect of Free Stream Turbulence (Bradshaw and Hancock)
 Case F-0231: Turbulent Boundary Layers on Surfaces of Mild Longitudinal Curvature (Hoffmann and Bradshaw)

- (Hoffmann and Bradshaw)
 Case F-0233: Turbulent Boundary Layer on a Convex, Curved Surface (Gillis and Johnston)
 Case F-0234: Effects of Small Streamline Curvature on Turbulent Duct Flow (Hunt and
- Joubert)
 Case F-0235: The Effects of Short Regions of High Surface Curvature on Turbulent Boundary Layers (Convex 30 degrees) (Smits et al)

 o Corrected data for Case F-0235

- o Corrected data for Case F-0235
 Case F-0241: Zero Pressure Gradient Constant Injection (Andersen et al)
 Case F-0242: Adverse Pressure Gradient with Constant Suction (Andersen et al)
 Case F-0244: Zero Pressure Gradient with Constant Suction (Favre et al)
 Case F-0244: Zero Pressure Gradient with Constant Suction (Favre et al)
 Case F-0251: NLR Infinite Swept Wing Experiment
 Case F-0252: Part-Rotating Cylinder Experiment (Bissonnette et al)
 Case F-0253: Cylinder on a Flat Test Plate (Dechow and Felsch)
 Case F-0254: Part-Rotating Cylinder (Lohmann)
 Case F-02561: Turbulent Wall jet Data Collected from Various Sources
 Case F-0311: Planar Mixing Layer Developing from Turbulent Wall Boundary Layers
 Case F-0231: The Turbulence Structure of a Highly Cyrinded Mixing Layer (Castro)

etc...

Data from Other Experiments

- Experimental data posted (or linked) here
 - For data that may be useful for RANS development or validation

Experimental Data

- Common Research Model (NASA) (independent website, will open new window)
 Shock Wave / Turbulent Boundary Layer Flows at High Mach Numbers (CUBRC) (independent website, will open new window)
- 2-D Coanda Airfoil with Tangential Wall Jet (under construction)
 Round Synthetic Jets for Separation Control on 2-D Ramp

- FAITH Hill 3-D Separated Flow
 Flow Behind a NACA 0012 Wingtip
 Shock Boundary Layer Interaction at M=2.05
 Various Hypersonic Shock Boundary Layer Interactions (NASA/TM-2013-216604)
 Planar Turbulent Wake in Various Pressure Gradients

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Data from Other DNS

DNS data posted (or linked) here

For data that may be useful for RANS development or validation

Incompressible Flow Cases

- Channel Flow of Jimenez et al (independent website, will open new window)
- Boundary Layer Flow of Jimenez et al (independent website, will open new window)
 3-D "Cherry" Diffuser (independent website, will open new window)
- Converging-Diverging Channel, Re=12600
- High-Order Moments in Unstrained and Strained Channel Flow

Compressible Flow Cases

- Compressible Supersonic Isothermal-Wall Channel Flow
- Compressible Periodic Hill <- new!

Data from Other LES

- LES data posted (or linked) here
 - For data that may be useful for RANS development or validation

Incompressible Flow Cases

- Coanda Airfoil with Tangential Wall Jet
- Periodic Hill
- Curved Backward-Facing Step
- NASA Wall-Mounted Hump
- Converging-Diverging Channel, Re=20580

Compressible Flow Cases

NASA Wall-Mounted Hump <- new!

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Turbulent Manufactured Solutions

- From Eca (used with permission)
- Used for series of V&V workshops at IST (Lisbon)

Information from Lisbon "Workshop on CFD Uncertainty Analysis" series

This web page provides some information from a series of turbulence-related Validation and Verification workshops held in Lisbon, Portugal, at the Instituto Superior Tecnico (IST). It includes manufactured solutions for wall-bounded incompressible turbulent flow. Everything on this page was provided courtesy of the workshop organizer <u>Luis Eca</u>, of IST. NASA assumes no responsibility for the accuracy of this information; questions should be directed to the originator. Additional details about the three workshops can be found in the American Institute of Aeronautics and Astronautics papers AIAA-2005-4728 (Toronto, June 2005), AIAA-2007-4089 (Miami, June 2007), and AIAA-2009-3647 (San Antonio, June 2009). See also Int. J. Numer. Meth. Fluids 54:119-154, 2007 and Int. J. Computational Fluid Dynamics 21(3-4):175-188, 2007 for details on the construction of manufactured solutions for one- and two-equation eddy-viscosity turbulence models.

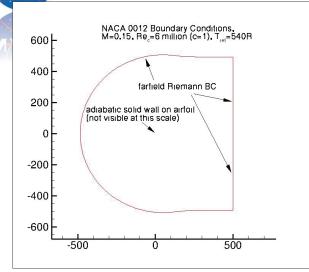
- Note describing test cases for the third workshop (pdf file)
- Note describing validation procedure for the third workshop (pdf file)
- Report IST D72-34 (2005), describing turbulent manufactured solutions for the workshop (pdf file)
- Report IST D72-36 (2006), describing turbulent manufactured solutions for the workshop (pdf
 file)
- Note describing manufactured functions available (pdf file)
- Fortran files associated with the workshop (tarred and gzipped directory)

Turbulence Model Numerical Analysis

- Purpose: more in-depth analysis of particular cases
- Different / finer grids than those on validation pages
- 8 cases have been built up to date
 - Coordinated with FDTC Solver Technology for Turbulent Flows DG
 - Currently focused on SA model only
 - Attempts to establish "reference solutions"
 - Handy for evaluating high-order schemes, novel numerical schemes, grid adaption, etc.
- See, e.g., Diskin et al.:
 - AIAA Journal, Vol. 54, No. 9, 2016, pp. 2563-2588
 - AIAA-2015-1746
 - AIAA-2018-1102

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Numerical Analysis – NACA 0012 with SA model



alpha=10 deg

0.08

FUN3D
CFL3D, 2nd order turb advection
CFL3D, 1st order turb advection
CFL3D, 1st order turb advection

0.02

solid line = finest grid
dashed = 1 level coarser
dash-dot = 2 levels coarser
dash-dot-dot = 3 levels coarser

0

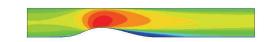
500
1000

- Based on grid convergence study results (using over 14 million grid points) and 3 codes (plus others in AIAA special session SciTech 2015), we have a good sense of the "reference solution", even without clear asymptotic rates of convergence
 - E.g., CL to within 0.0002, or 0.02%
 - E.g., CD to within 0.00001, or 1/10th drag count

Includes additional analysis of streamwise grid resolution influence near T.E.



http://turbmodels.larc.nasa.gov



- TMR seeks to bring consistency to the testing, verification, and validation of RANS turbulence models for the CFD community
- One of biggest reason for its success may be its "openness"
 - By including all details (equations, grids, BCs, existing CFD results), it encourages quick comparisons and makes inter-organizational collaborations easier
 - Mistakes on the website are occasionally found by the community; its openness makes the process of finding and fixing them more efficient
 - TMBWG is an open working group; anyone can join

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TMR Open Questions

- How to find the time to verify/validate additional models for posting to TMR?
 - It is tedious, unglamorous work
 - Currently requires author's collaboration (NASA site is not a wiki)
- How to create stronger connection between the TMR and researchers with new RANS ideas?
 - Original hope for site: to facilitate the dissemination of new turbulence models to the community
 - To date, very few modelers have done this
- How to handle the fact that codes (and their results) might change over time?
- What about hybrid RANS-LES and LES models?
 - They can be described, but how to verify them?
 - New site (http://wmles.umd.edu/) is beginning to attempt this for wall-modeled LES (WMLES)



Summary

- Most workshops focusing on turbulence models have suffered from "same model... different code... different results" syndrome
 - Different model versions used, errors introduced, or undocumented features added
 - Muddies the workshop conclusions
- To make workshops more useful, codes should be <u>verified</u>
 - Via MMS, or...
 - NASA TMR website makes crude verification very easy for many modern RANS models SA, SA-RC, SST, SST-V, SST-2003, Wilcox2006, kkL-MEAH2015, SSG/LRR-RSM-w2012 (other models will eventually be added)
 - No additional coding needed; just run simple cases on sequence of grids provided, and compare against posted results
 - AIAA's DPW and HiLiftPW series have started to promote this way of thinking
- With verification done, we could focus on more important issues

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Important issues...

- Improved geometric fidelity
- Use of appropriate boundary conditions
- Better grids
 - Finer resolution
 - Improved quality
 - Automatic grid adaption
- Better numerics
 - Higher order accuracy
 - Better iterative convergence
- Improved physics
 - Transition
 - More widely applicable turbulence models (e.g., for separated flow)

Executive summary

- Use websites to encourage crowd-sourcing of ideas
 - Post data, grids, everything... make it <u>easy</u> for people to use your results and learn from them
 - Continue to invest in RANS research
 - Collective improvement through workshops, including <u>both</u> verification and validation
 - Verification prior to validation!





Move from this...

Which turbulence model Should I use? Which code?

well, you could use Model A in Code B if you want more separation, but the grid needs to be coarse, or else you'll get less separation, except on Tuesdays. Or Model A in Code C will give less separation, unless you get the developer's version of Code C. Or Model B in Code D could work if you edit the code and change Constant E by a factor of two...





... toward this

Which turbulence model should I use? Which code?

The models are all doesn't doe



