

Quantum Molecular Dynamics

- QMD (Quantum Molecular Dynamics) is quantum extension of classical molecular-dynamics model.
- Each nucleon is seen as a Gaussian wave packet
- Propagation with scattering term which take into account Pauli principals
- QMD model is widely used to analyze various aspects of heavy ion reactions.
- Especially for many-body processes in particular the formation of complex fragments which hard to treat with Vlasov-Uehling-Uhlenbeck (VUU) and Boltzmann-Uehling-Uhlenbeck (BUU) equations

Binary Light Ion Cascade

- This is an Ion extension of Binary Cascade
- In Binary Cascade
 - Participant nucleons are also represented by wave function and numerically calculated time development of Hamiltonian
 - The scattering term considers only binary collision and decay
 - However, Binary Cascade
 - Neglects participant-participant scattering potential
 - Uses simple time independent optical potential
 - Does not provide ground state nucleus which can be used in molecular dynamics
 - Recommended for use when either projectile or target is C12 or lighter (other particle can be heavier)

New native QMD code in Geant4

Koji Tatsumi
SLAC SCCC S



Derivation of the transport equation of QMD

- Wave function of each nucleon in the system
 - Total n-body wave function
 - Hamiltonian
 - Equations of motion for i-th particles
- $$\phi_i(x; q_i, p_i, t) = \left(\frac{2}{L\pi} \right)^{\frac{3}{4}} \exp \left\{ -\frac{2}{L} (x - q_i(t))^2 + \frac{i}{\hbar} p_i(t) x \right\}$$
- $$H = \sum_i T_i + \sum_{ij} V_{ij}$$
- $$\dot{p}_i = - \frac{\partial \langle H \rangle}{\partial q_i} \quad \text{and} \quad \dot{q}_i = \frac{\partial \langle H \rangle}{\partial p_i}$$

G4QMD

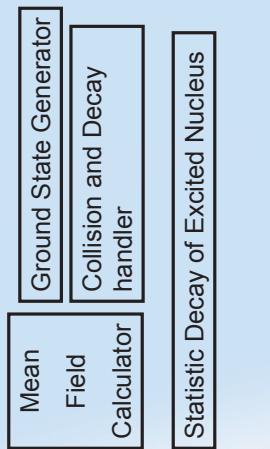
The solution for overcoming limitation of Binary Light Ion Cascade, and enable to simulate real HZE reactions

- G4QMD create ground state nucleus based on JQMD, which can be used in MD
- Potential field and field parameters of G4QMD is also based on JQMD with Lorentz scalar modifications
 - "Development of Iaeri QMD Code" Niita et al, JAERI-Data/Code 99-042
- Self generating potential field is used in G4QMD
- G4QMD uses scatter and decay library of Geant4
- Following resonances are taken into account
 - Δ_{1332} , Δ_{1600} , Δ_{1620} , Δ_{1700} , Δ_{1900} , Δ_{1910} , Δ_{1920} , Δ_{1930} and Δ_{1950}
 - N_{1400} , N_{1520} , N_{1533} , N_{1650} , N_{1673} , N_{1680} , N_{1700} , N_{1710} , N_{1720} , N_{1900} , N_{2090} , N_{2190} , N_{2220} and N_{2250}
- G4QMD includes Participant-Participant Scattering
- After the QMD reaction calculation G4QMD connects to Evaporation Models of Geant4

G4HadronicInteraction



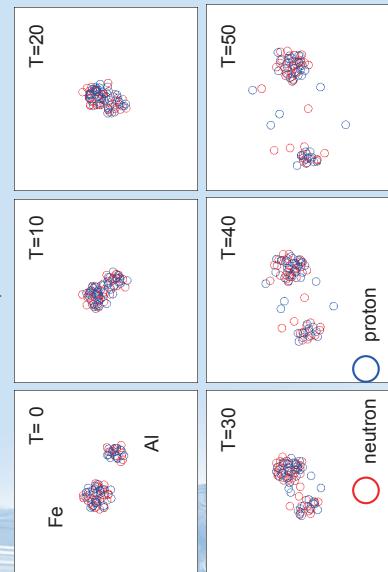
G4QMDReactionModel



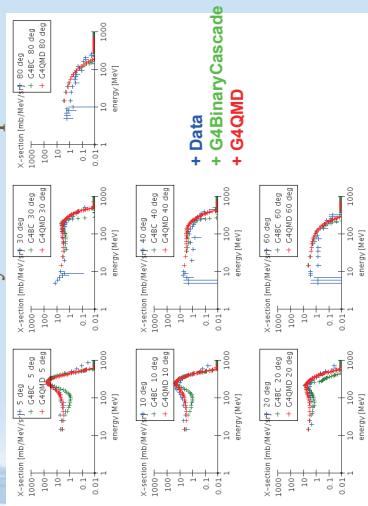
Other features

- Automatic Extension of time steps for relatively slow projectiles.
- Acceleration by Coulomb potential of final state particles is taken into account.
- Above features are incorporated by fruitful discussions with Vanderbilt Univ. group

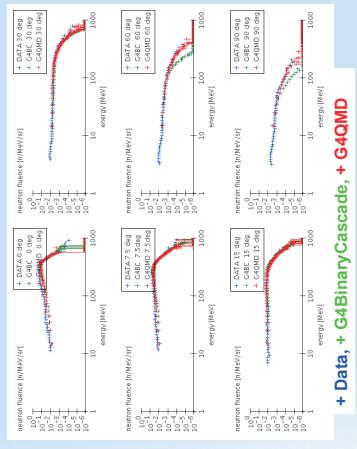
QMD Calculation Fe 290MeV/n on Al



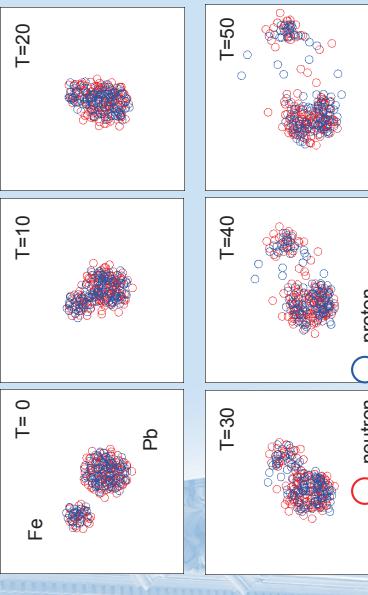
C12 290MeV/n on Carbon Secondary neutron spectra



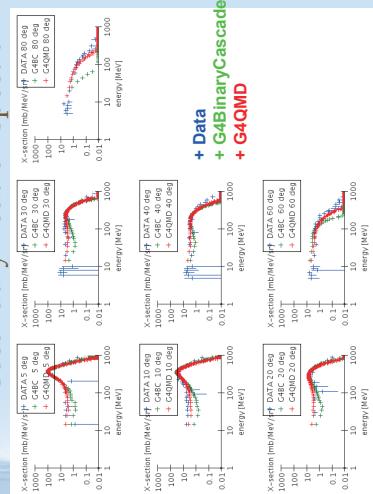
Fe56 400MeV/n on Thick Aluminum Neutron Yield

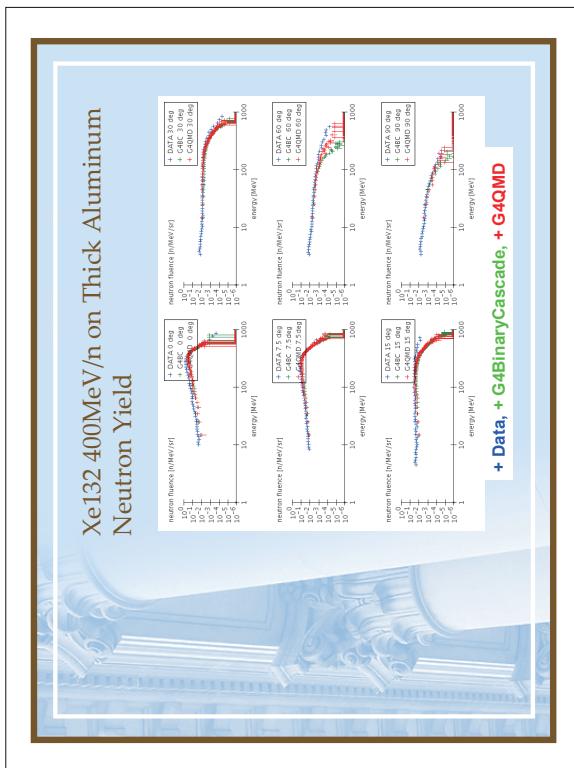
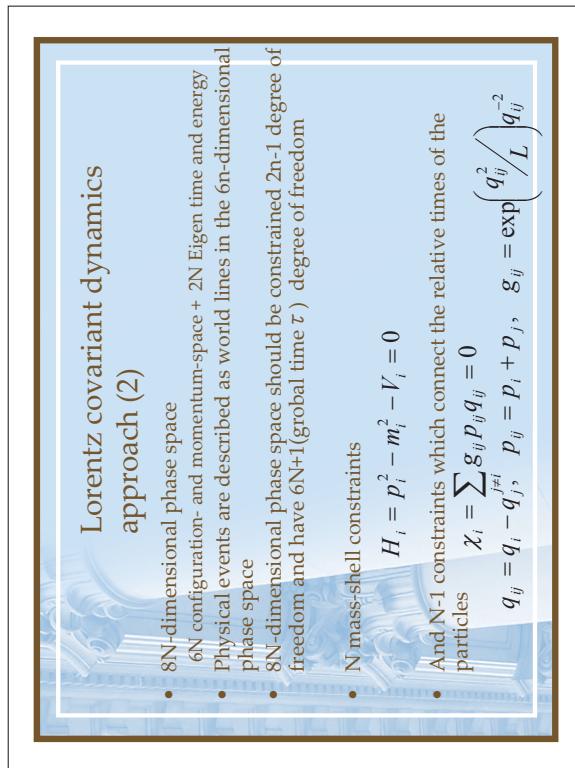
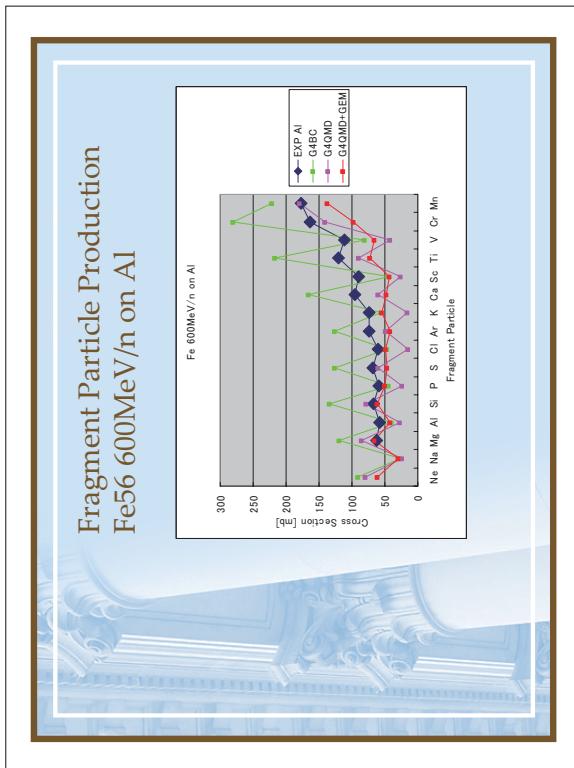


QMD Calculation Fe 290MeV/n on Pb



Ne20 400MeV/n on Carbon Secondary neutron spectra





Lorentz covariant dynamics approach (3)

- Hamiltonian
$$H = \sum_{i=1}^N \lambda_i H_i + \sum_{i=1}^{N-1} \delta\mu_i \chi_i$$
- Equations of motion
$$\frac{dq_j}{d\tau} = \frac{\partial H}{\partial p_j} = 2\lambda_j p_j - \sum_{i=1}^N \lambda_i \frac{\partial V_i}{\partial p_j}$$

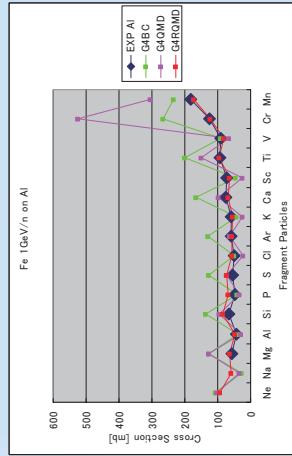
$$\frac{dp_j}{d\tau} = -\frac{\partial H}{\partial q_j} = \sum_{i=1}^N \lambda_i \frac{\partial V_i}{\partial q_j}$$
with the coefficients λ_i

Lorentz covariant dynamics approach (4)

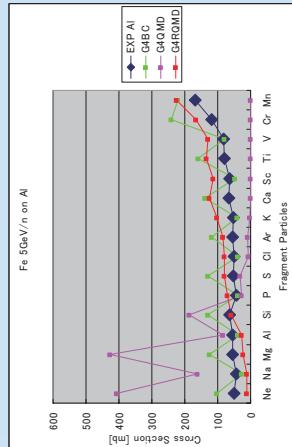
- And λ_i is
$$\lambda_j \approx -\frac{\partial \chi_N}{\partial \tau} S_{Ni}$$

$$(S^{-1})_{ij} \equiv \{H_i, \chi_j\}_{\text{Poisson bracket}}$$
 - In order to solve the equations of motion one needs to calculate the coefficients λ_i . For their calculation the matrix S^{-1} must be inverted.
- Reference
Poincaré invariant Hamiltonian dynamics: Modelling multi-hadronic interactions in a phase space approach. H. Sorge, H. Stocker and W. Greiner. *Ann. Phys.* 192, 266 1989
Microscopic Models for Ultrarelativistic Heavy Ion Collisions S. A. Bass et al., *Prog. Part. Nucl. Phys.* 41, 225 1998

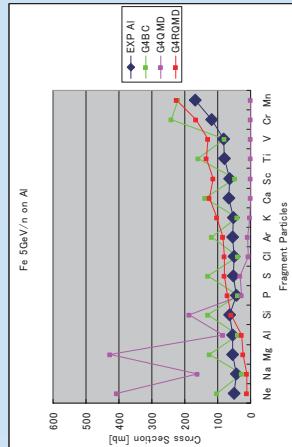
Validation of G4RQMD Fe 1GeV/n on Al



Validation of G4RQMD Fe 5GeV/n on Al



Validation of G4RQMD Fe 5GeV/n on Al



Summary

- We are developing G4QMD which handle nucleus-nucleus interaction up to $\sim 5 \text{ GeV/n}$
 - Validation shows much improved results than Binary (Light ion) Cascade
 - The first (alpha) release was done in Geant4 v9.1
- We are also developing G4RQMD which has Lorentz covariant dynamics.
- First validation of G4RQMD shows quite promising results in relativistic energy collisions
 - However there still remain many points of improvements and further developments.